

Solid State Detectors

Most material is taken from lectures by Michael Moll/CERN and Daniela Bortoletto/Purdue and the book 'Semiconductor Radiation Detectors' by Gerhard Lutz.

In gaseous detectors, a charged particle is liberating electrons from the atoms, which are freely bouncing between the gas atoms.

An applied electric field makes the electrons and ions move, which induces signals on the metal readout electrodes.

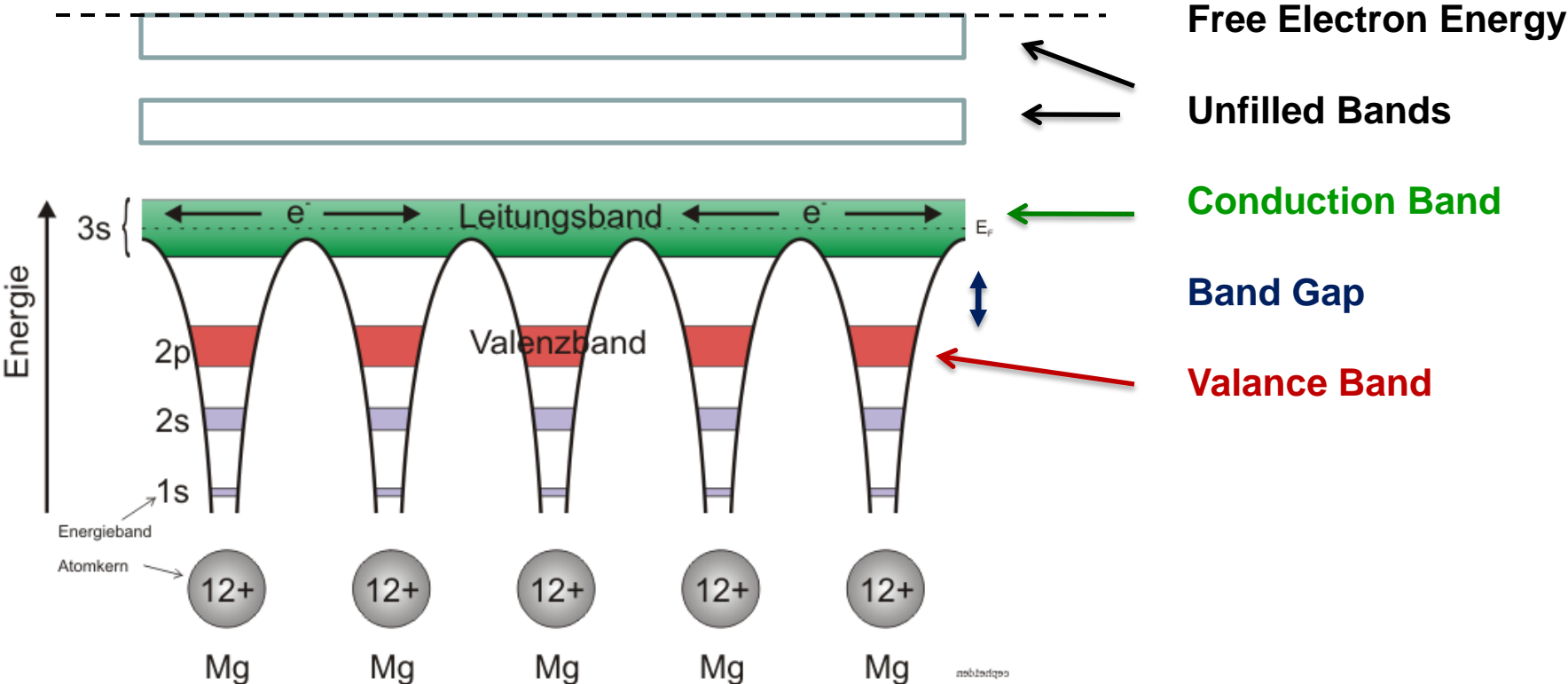
For individual gas atoms, the electron energy levels are discrete.

In solids (crystals), the electron energy levels are in 'bands'.

Inner shell electrons, in the lower energy bands, are closely bound to the individual atoms and always stay with 'their' atoms.

In a crystal there are however energy bands that are still bound states of the crystal, but they belong to the entire crystal. Electrons in this bands and the holes in the lower band can freely move around the crystal, if an electric field is applied.

Solid State Detectors



Solid State Detectors

In case the conduction band is filled the crystal is a conductor.

In case the conduction band is empty and 'far away' from the valence band, the crystal is an insulator.

In case the conduction band is empty but the distance to the valence band is small, the crystal is a semiconductor.

The energy gap between the last filled band – the valence band – and the conduction band is called band gap E_g .

The band gap of Diamond/Silicon/Germanium is 5.5, 1.12, 0.66 eV.

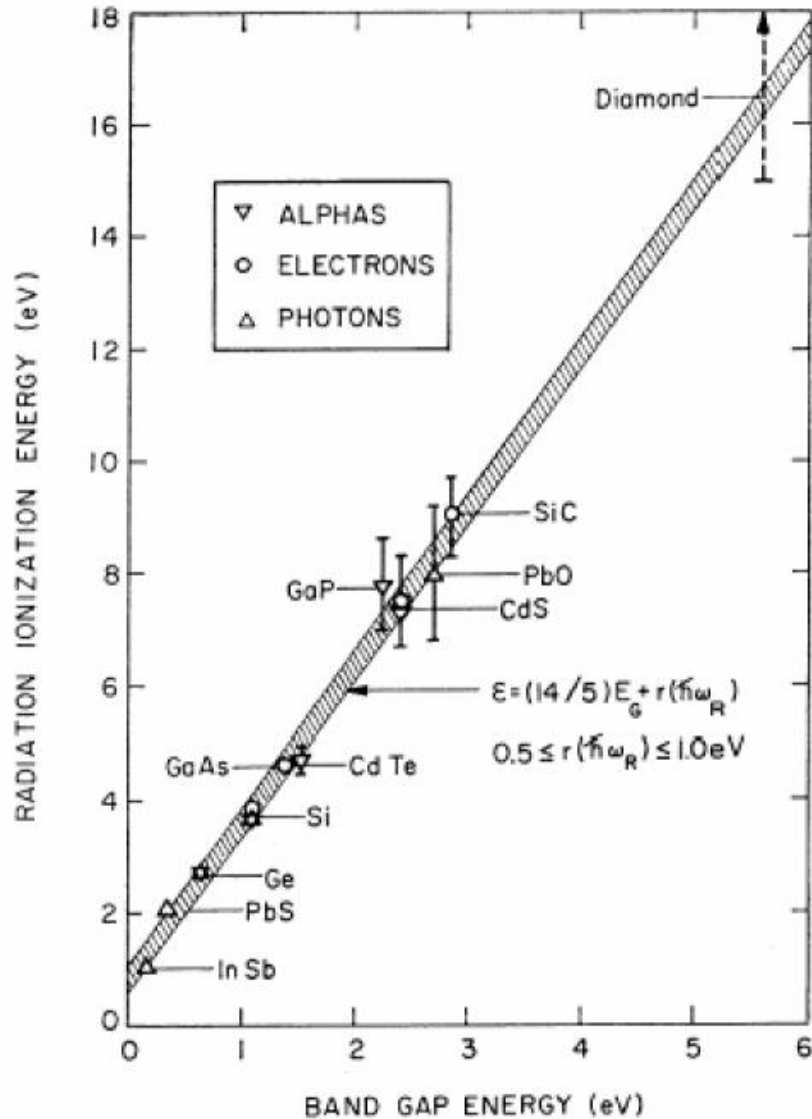
The average energy to produce an electron/hole pair for Diamond/Silicon/Germanium is 13, 3.6, 2.9eV.

In case an electron in the valence band gains energy by some process, it can be excited into the conduction band and a hole in the valence band is left behind.

Such a process can be the passage of a charged particle, but also thermal excitation → probability is proportional $\text{Exp}(-E_g/kT)$.

The number of electrons in the conduction band is therefore increasing with temperature i.e. the conductivity of a semiconductor increases with temperature.

Solid State Detectors



	Diamond	SiC (4H)	GaAs	Si	Ge
Atomic number Z	6	14/6	31/33	14	32
Bandgap E_g [eV]	5.5	3.3	1.42	1.12	0.66
$E(\text{e-h pair})$ [eV]	13	7.6-8.4	4.3	3.6	2.9
density [g/cm ³]	3.515	3.22	5.32	2.33	5.32
e-mobility μ_e [cm ² /Vs]	1800	800	8500	1450	3900
h-mobility μ_h [cm ² /Vs]	1200	115	400	450	1900

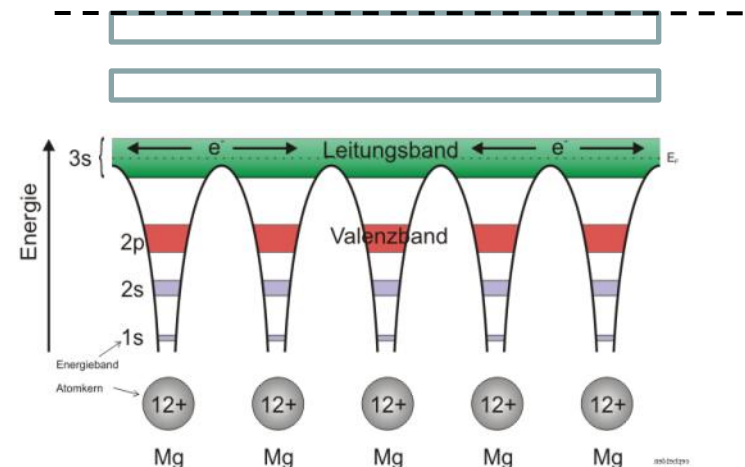
Solid State Detectors

It is possible to treat electrons in the conduction band and holes in the valence band similar to free particles, but with an effective mass different from elementary electrons not embedded in the lattice.

This mass is furthermore dependent on other parameters such as the direction of movement with respect to the crystal axis. All this follows from the QM treatment of the crystal.

If we want to use a semiconductor as a detector for charged particles, the number of charge carriers in the conduction band due to thermal excitation must be smaller than the number of charge carriers in the conduction band produced by the passage of a charged particle.

Diamond ($E_g=5.5\text{eV}$) can be used for particle detection at room temperature, Silicon ($E_g=1.12\text{eV}$) and Germanium ($E_g=0.66\text{eV}$) must be cooled, or the free charge carriers must be eliminated by other tricks \rightarrow doping \rightarrow see later.



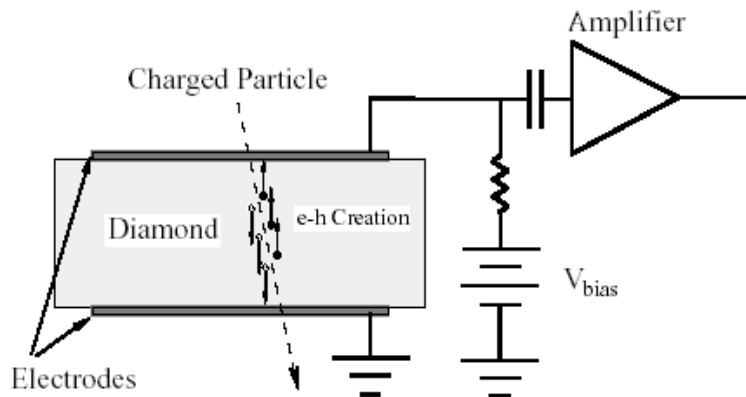
Solid State Detectors

The average energy to produce an electron/hole pair for Diamond/Silicon/Germanium is 13, 3.6, 2.9eV.

Comparing to gas detectors, the density of a solid is about a factor 1000 larger than that of a gas and the energy to produce an electron/hole pair e.g. for Si is a factor 7 smaller than the energy to produce an electron-ion pair in Argon.

The number of primary charges in a Si detector is therefore about 10^4 times larger than the one in gas → while gas detectors need internal charge amplification, solid state detectors don't need internal amplification.

While in gaseous detectors, the velocity of electrons and ions differs by a factor 1000, the velocity of electrons and holes in many semiconductor detectors is quite similar.

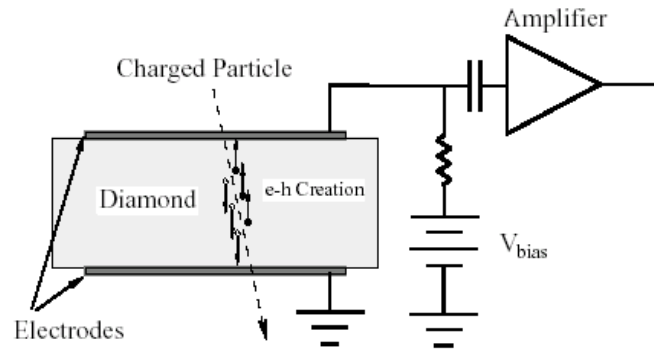


Diamond → A solid state ionization chamber

Diamond Detector

Typical thickness – a few 100 μm .

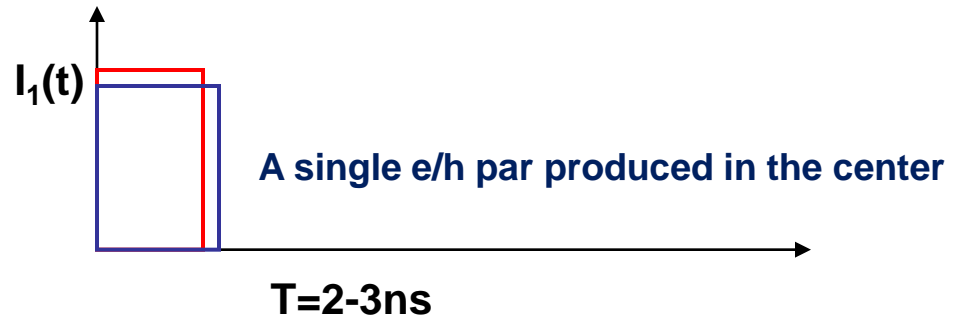
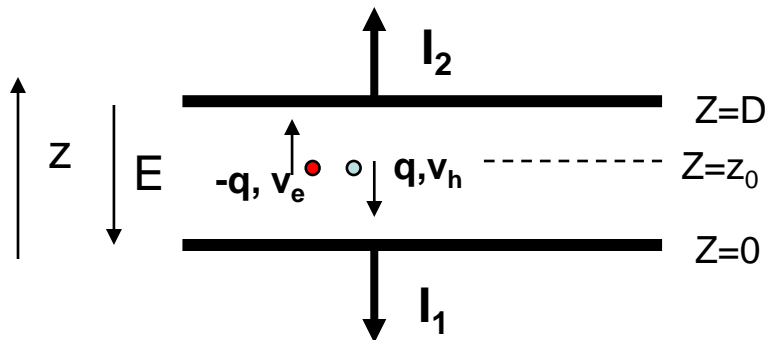
<1000 charge carriers/cm³ at room temperature due to large band gap.



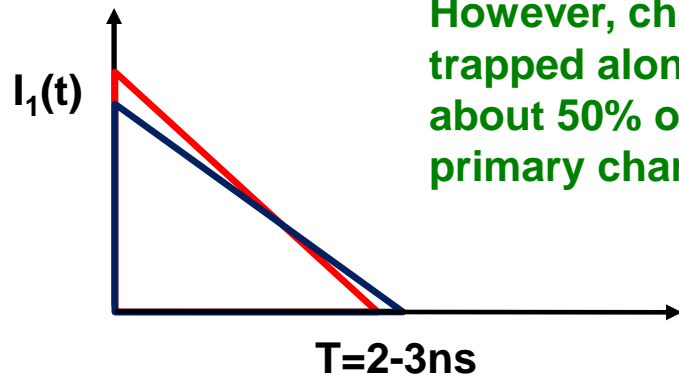
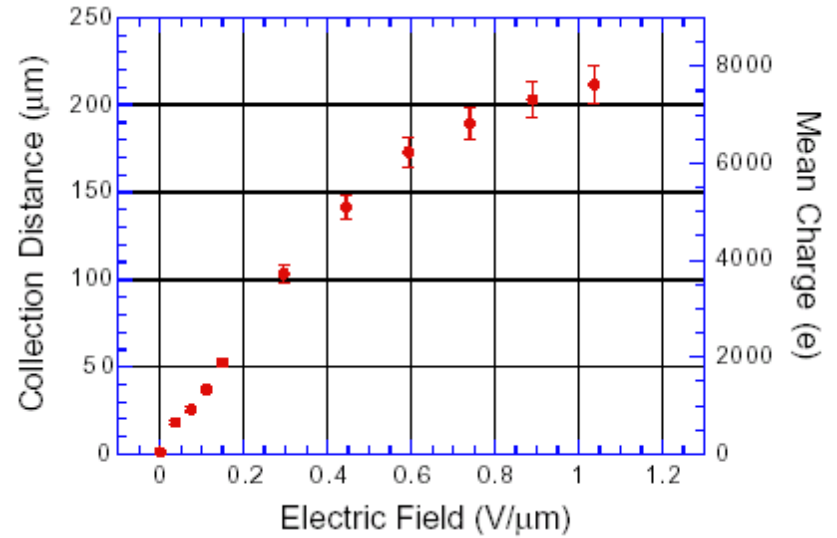
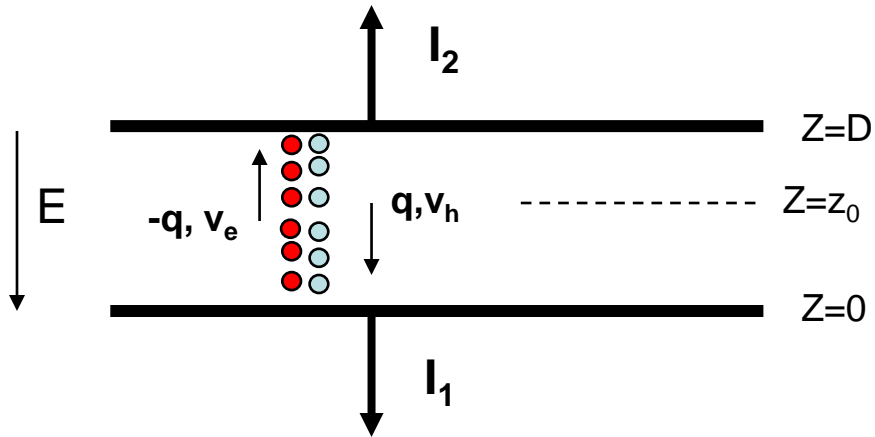
Velocity:

$\mu_e=1800 \text{ cm}^2/\text{Vs}$, $\mu_h=1600 \text{ cm}^2/\text{Vs}$

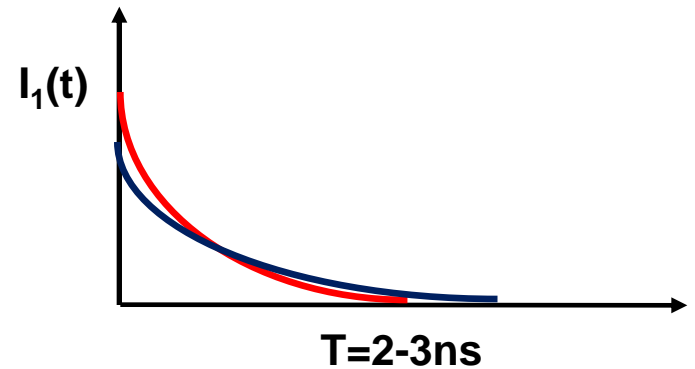
Velocity = μE , 10kV/cm $\rightarrow v=180 \mu\text{m}/\text{ns} \rightarrow$ Very fast signals of only a few ns length !



Diamond Detector



However, charges are trapped along the track, only about 50% of *produced* primary charge is *induced* \rightarrow



Silicon Detector

Velocity:

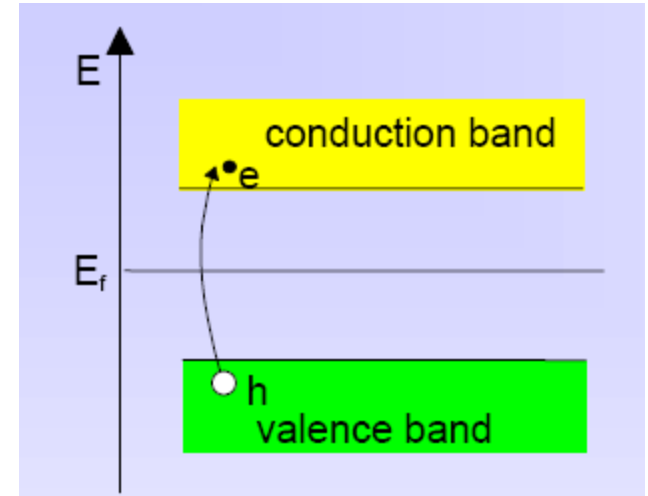
$\mu_e=1450 \text{ cm}^2/\text{Vs}$, $\mu_h=505 \text{ cm}^2/\text{Vs}$, 3.63eV per e-h pair.

~11000 e/h pairs in 100 μm of silicon.

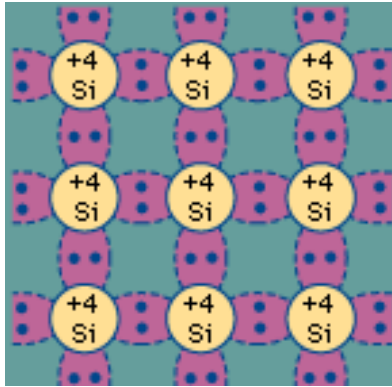
However: Free charge carriers in Si:

T=300 K: $n/h = 1.45 \times 10^{10} / \text{cm}^3$ but only 33000e-/h in 300 μm produced by a high energy particle.

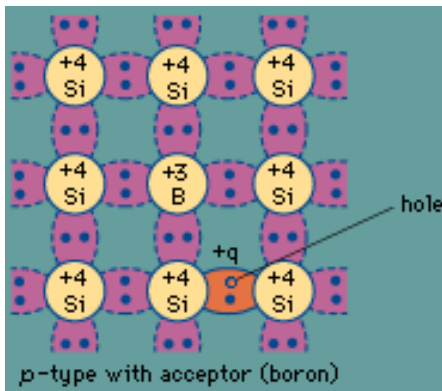
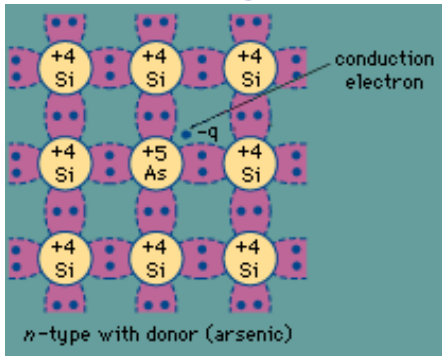
Why can we use Si as a solid state detector ???



Doping of Silicon



doping

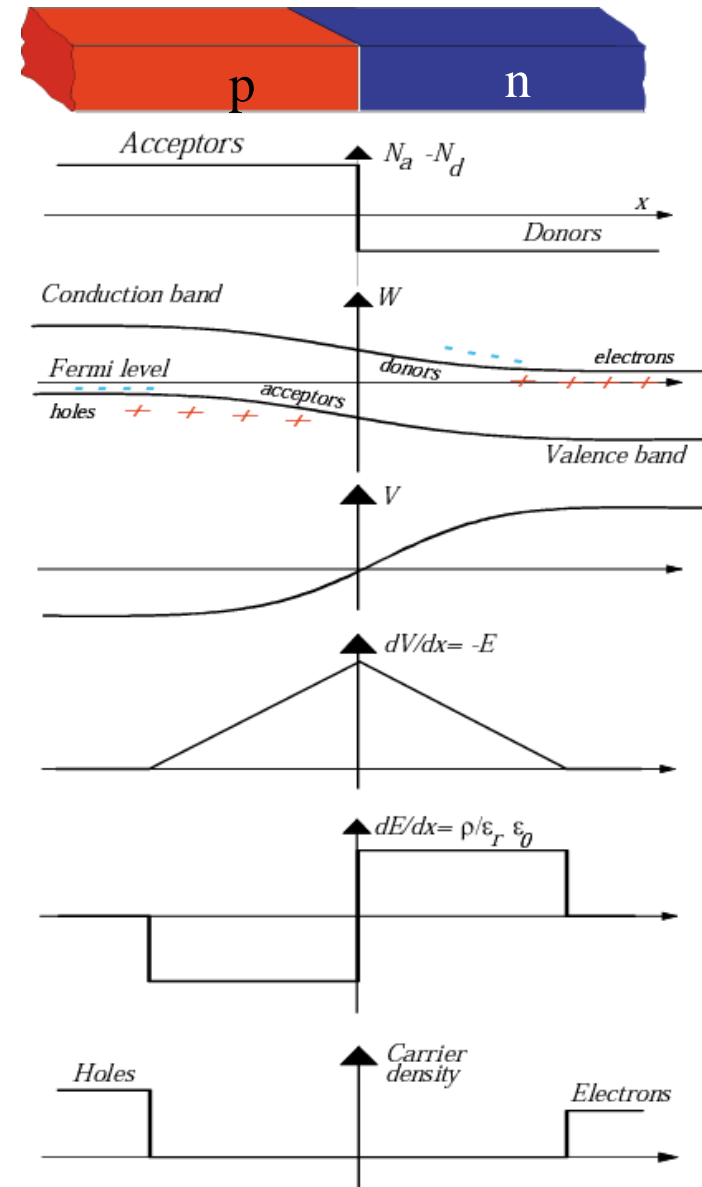


In a silicon crystal at a given temperature the number of electrons in the conduction band is equal to the number of holes in the valence band.

Doping Silicon with Arsen (+5) it becomes and n-type conductor (more electrons than holes).

Doping Silicon with Boron (+3) it becomes a p-type conductor (more holes than electrons).

Bringing p and n in contact makes a diode.



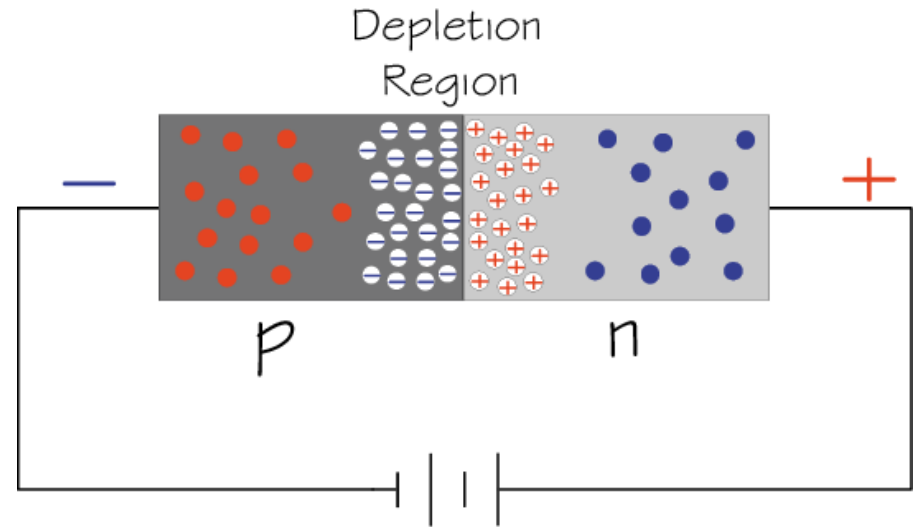
Si-Diode used as a Particle Detector !

At the p-n junction the charges are depleted and a zone free of charge carriers is established.

By applying a voltage, the depletion zone can be extended to the entire diode → highly insulating layer.

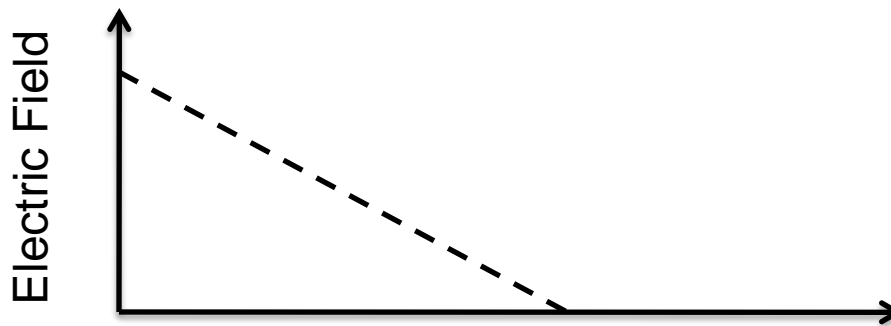
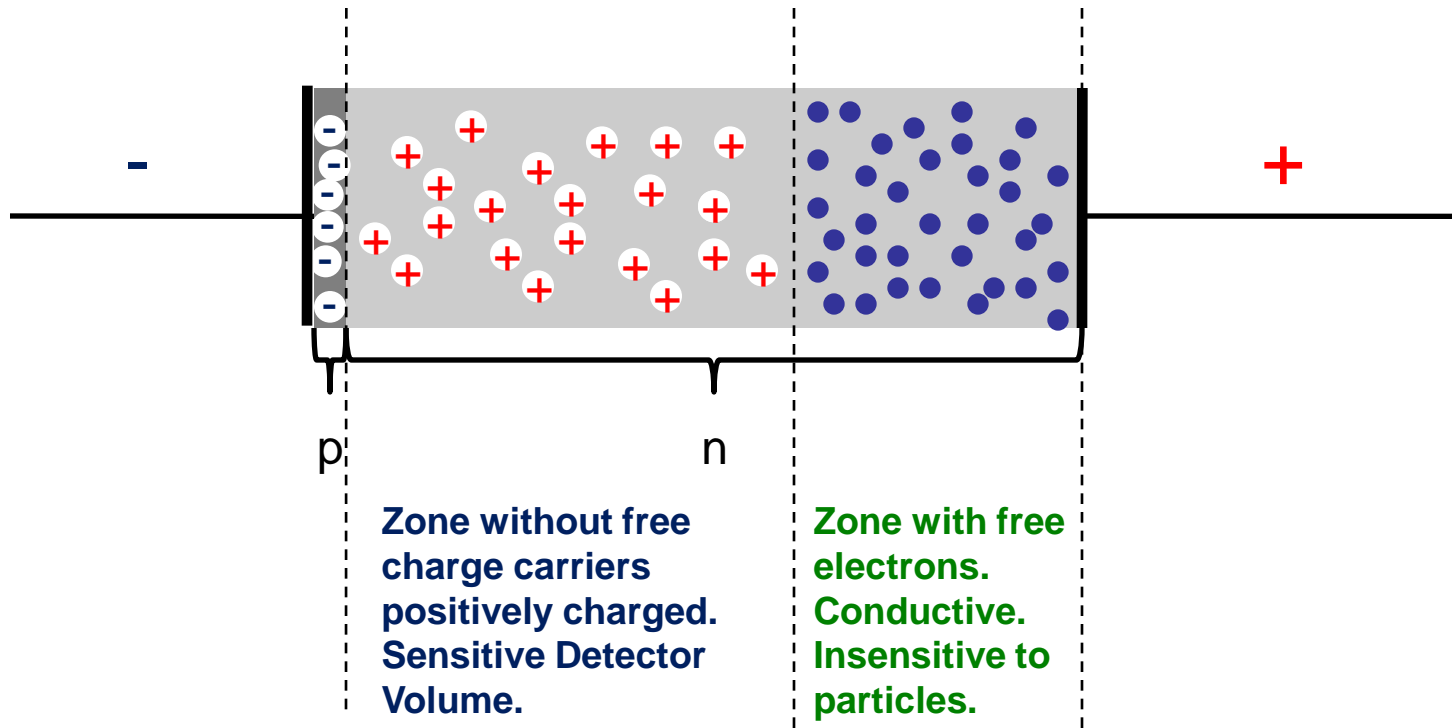
An ionizing particle produces free charge carriers in the diode, which drift in the electric field and induce an electrical signal on the metal electrodes.

As silicon is the most commonly used material in the electronics industry, it has one big advantage with respect to other materials, namely highly developed technology.

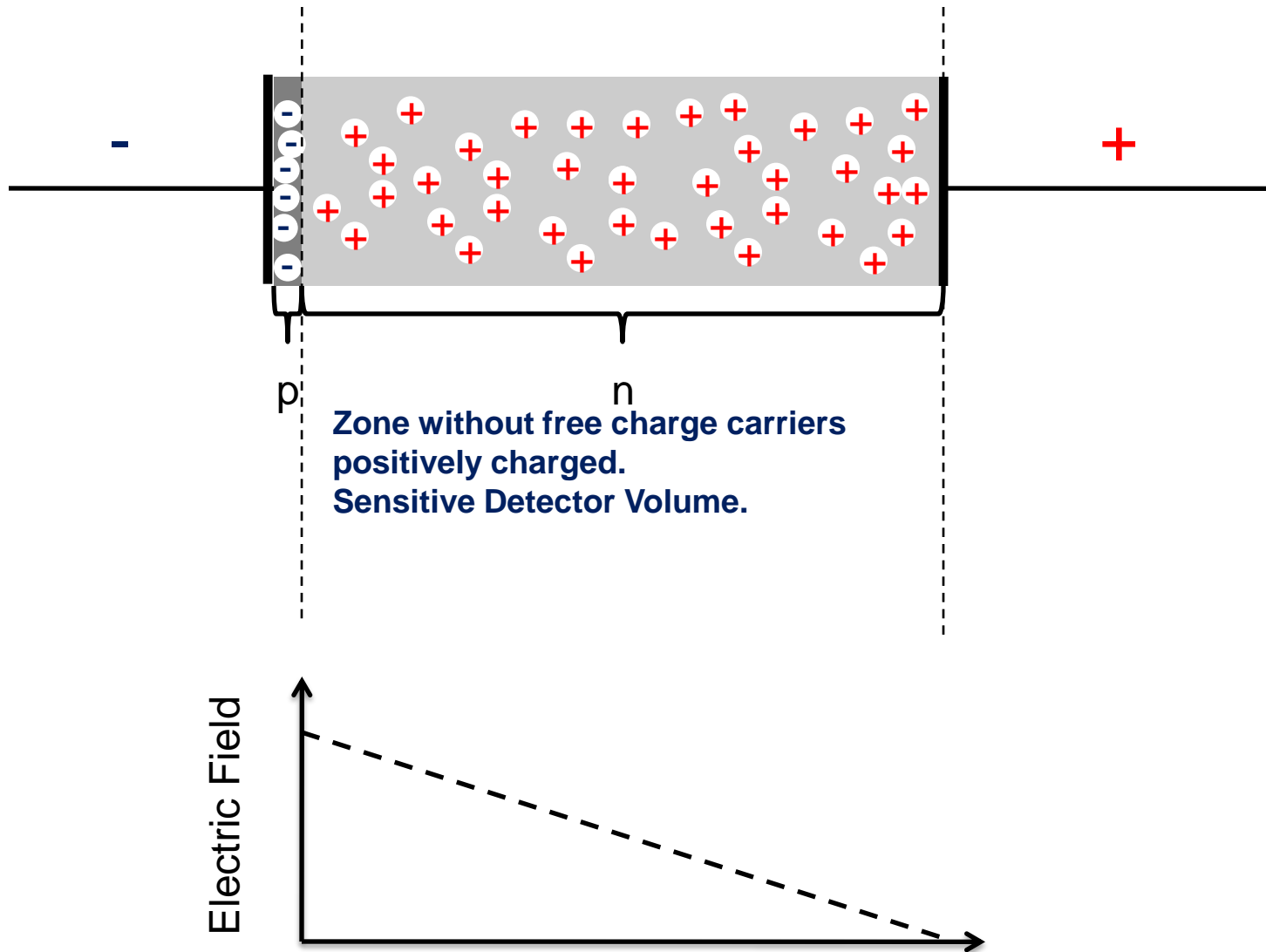


- Electron
- ⊕ Positive ion from removal of electron in n-type impurity
- ⊖ Negative ion from filling in p-type vacancy
- Hole

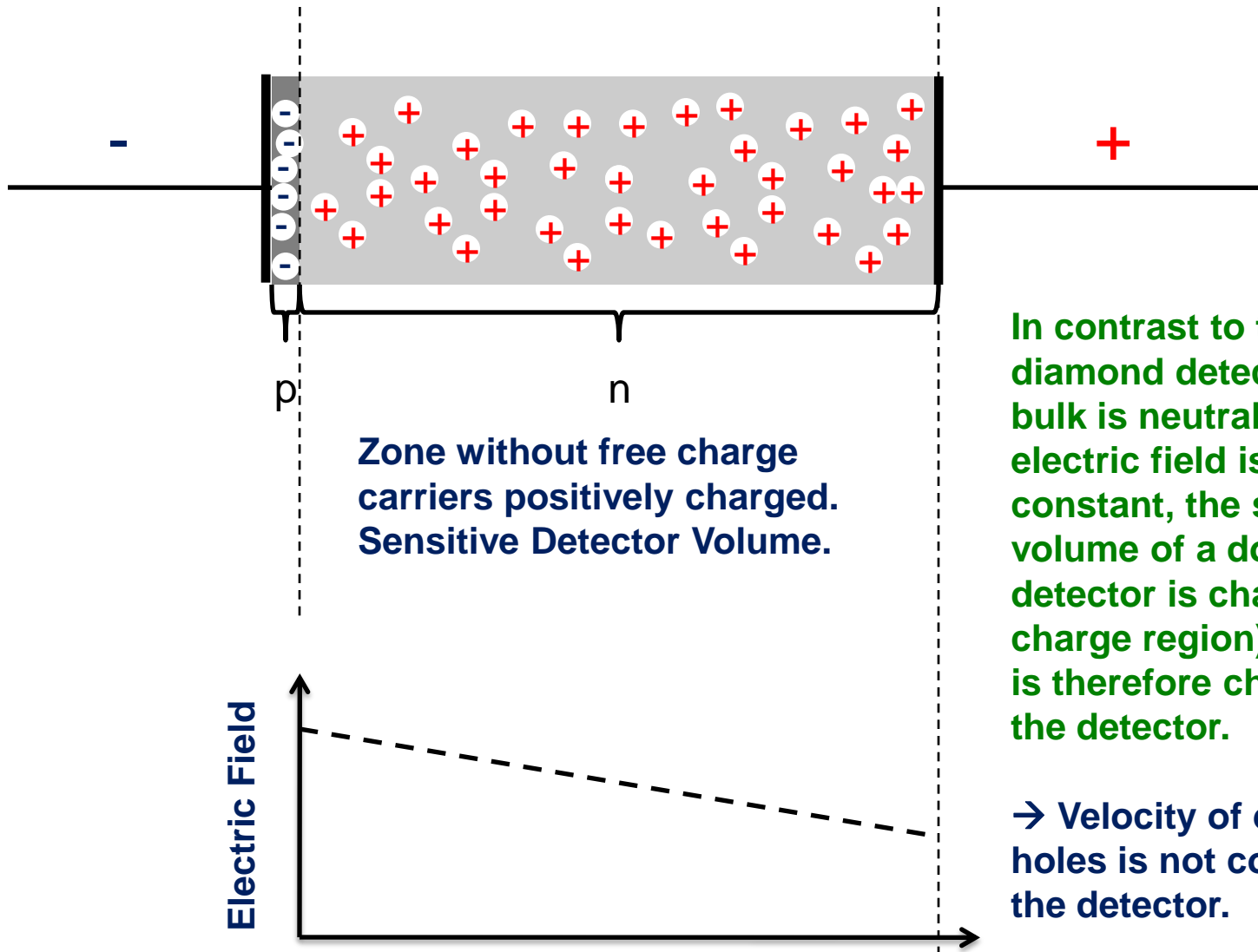
Under-Depleted Silicon Detector



Fully-Depleted Silicon Detector



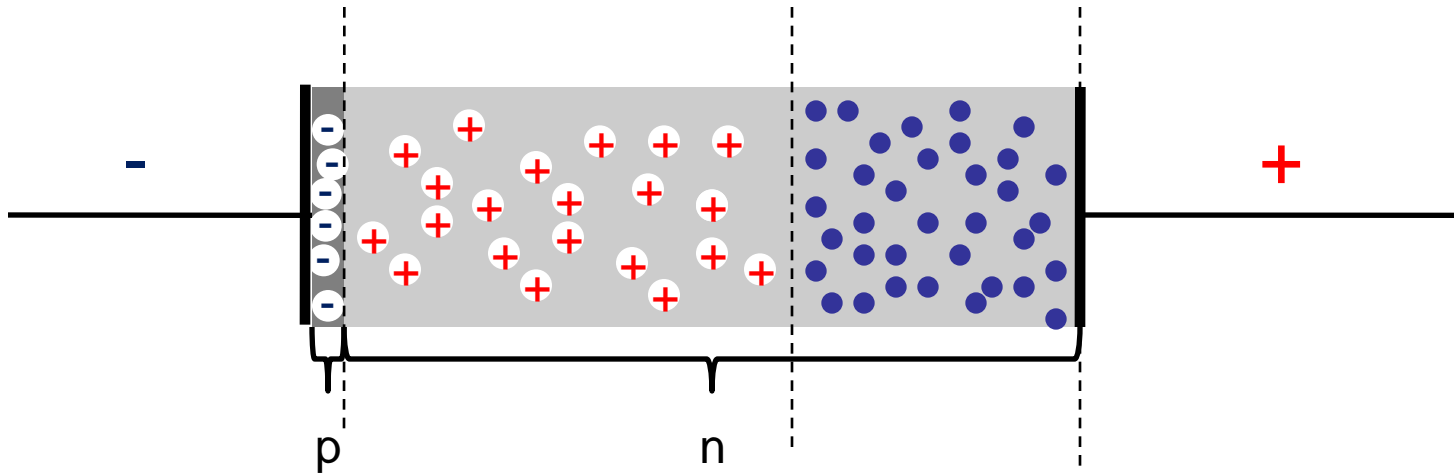
Over-Depleted Silicon Detector



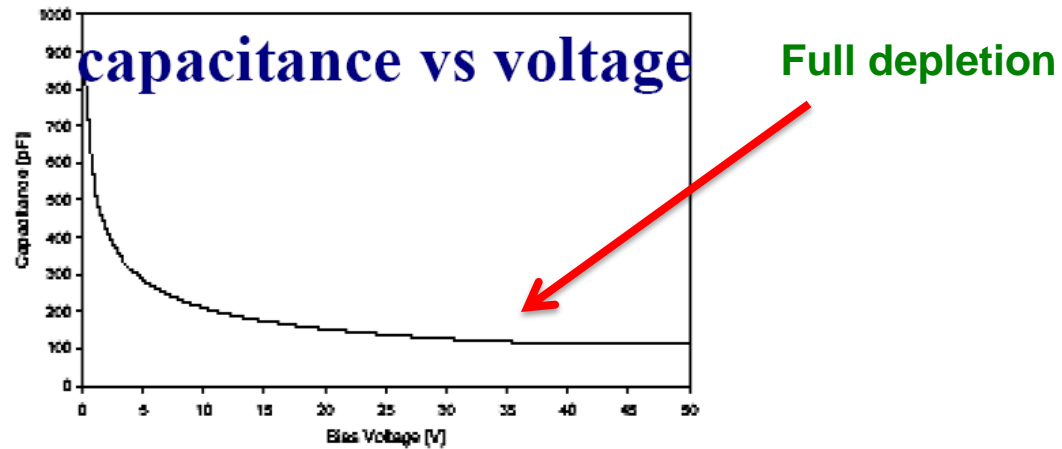
In contrast to the (un-doped) diamond detector where the bulk is neutral and the electric field is therefore constant, the sensitive volume of a doped silicon detector is charged (space charge region) and the field is therefore changing along the detector.

→ Velocity of electrons and holes is not constant along the detector.

Depletion Voltage



The capacitance of the detector decreases as the depletion zone increases.

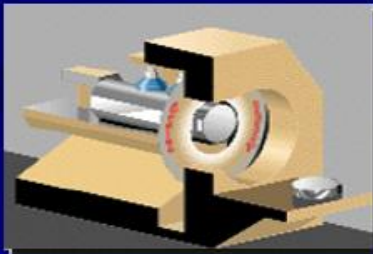
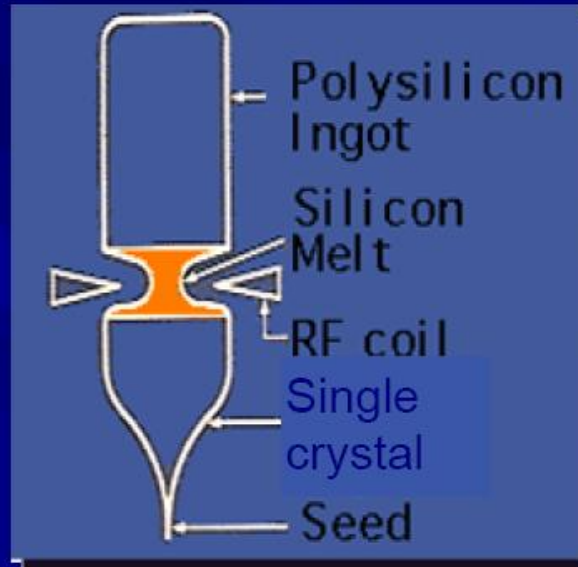


Wafer Fabrication

1) Start with very pure quartzite sand. Clean it and further purify by chemical processes. Melt it and add the tiny concentration of phosphorus (boron) dopant to make n(p) type silicon. Pour it in a mold to make a polycrystalline silicon cylinder



2) Using a single silicon crystal seed, melt the vertically oriented polycrystalline cylinder onto the seed using RF power to obtain single crystal 'ingot'.



3) Slice ingot into wafers of thickness 300-500 μ m with diamond encrusted wire or disc saws.

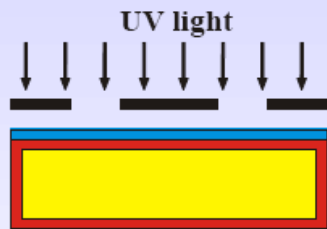
A "simple" production sequence (schematic)

n-type silicon

- Polished n-type silicon wafer (typical $\rho \sim 1-10 \text{ K}\Omega\text{cm}$)



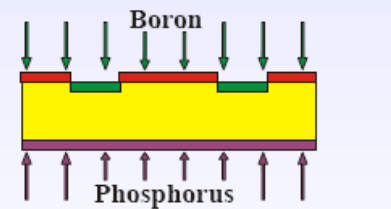
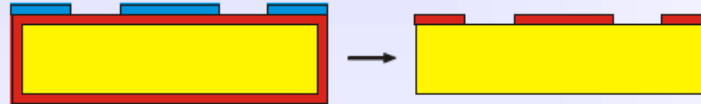
- Oxidation (800-1200°C)



- Photolithography (coat with photo resist; align mask, expose to UV light, develop photoresist);

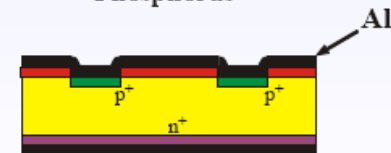
Etching of oxide

etch

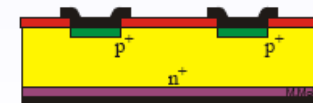


- Doping with boron and phosphorus by implantation (or by diffusion)
Annealing to cure radiation damage and activate dopants

- p⁺ n junction on front side
- n n⁺ ohmic contact on back side



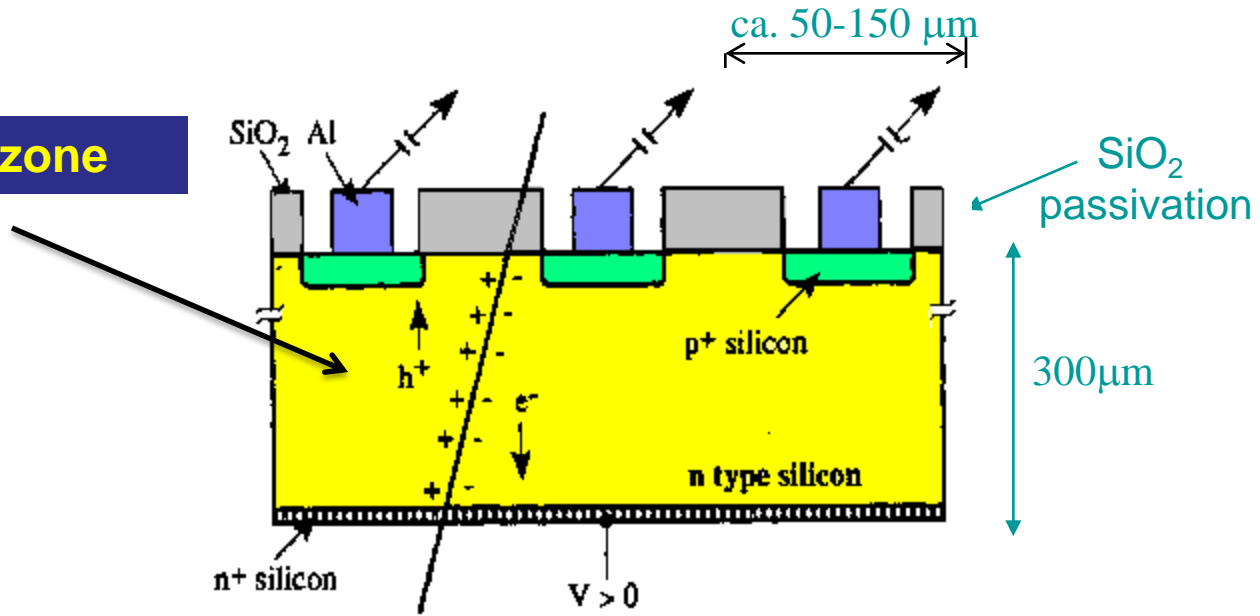
- Aluminize surface (e.g. by evaporation)



- Pattern metal for diode contacts

Silicon Detector

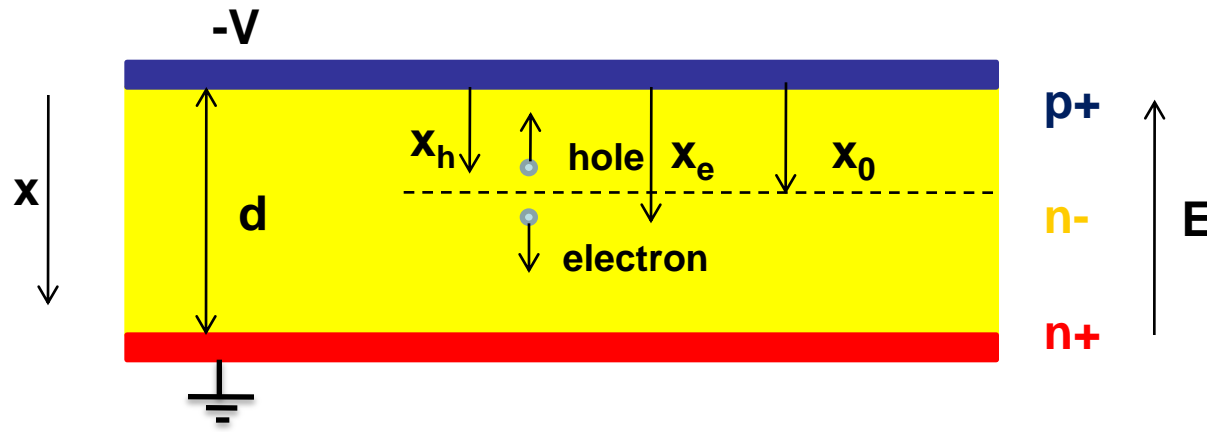
Fully depleted zone



$N(e-h) = 11\ 000/100\mu\text{m}$

Position Resolution down to $\sim 5\mu\text{m}$!

What is the Signal induced on the p+ layer ?



What is the signal induced on the p+ 'electrode' for a single e/h pair created at $x_0=d/2$ for a 300um Si detector ?

$$E(x) = - \left[2 \frac{d-x}{d^2} V_{dep} + \frac{V - V_{dep}}{d} \right] \quad v_e(x) = \mu_e E(x) \quad v_h(x) = \mu_h E(x)$$

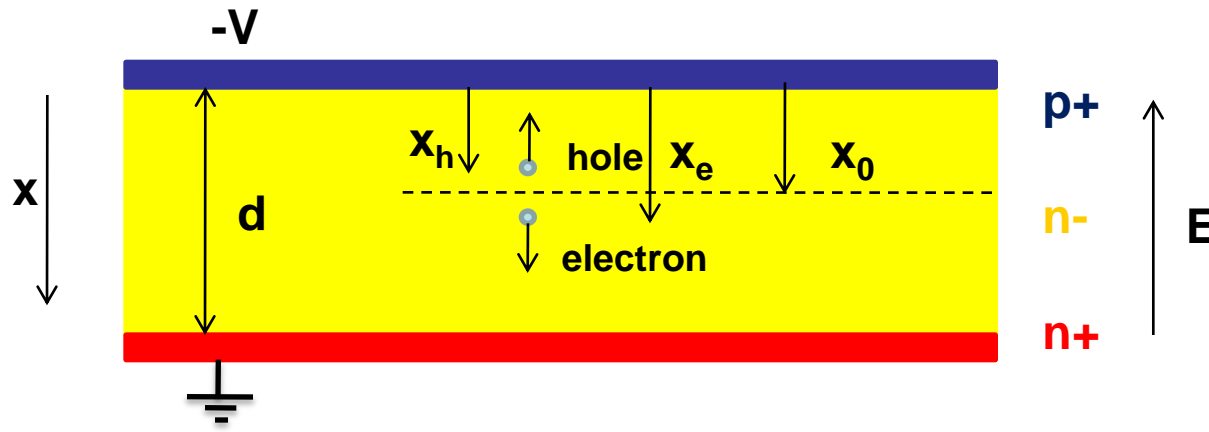
$$\frac{dx_e(t)}{dt} = \mu_e E(x(t)) \quad x_e(t) = d \frac{V + V_{dep}}{2V_{dep}} + \left[x_0 - d \frac{V + V_{dep}}{2V_{dep}} \right] e^{-2\mu_e V_{dep} t / d^2}$$

$$\frac{dx_e(t)}{dt} = \mu_e \left[\frac{2V_{dep}}{d^2} x_0 - \frac{V + V_{dep}}{d} e^{-2\mu_e V_{dep} t / d^2} \right]$$

$$\frac{dx_h(t)}{dt} = -\mu_h E(x(t)) \quad x_h(t) = d \frac{V + V_{dep}}{2V_{dep}} + \left[x_0 - d \frac{V + V_{dep}}{2V_{dep}} \right] e^{2\mu_h V_{dep} t / d^2}$$

$$\frac{dx_h(t)}{dt} = \mu_h \left[\frac{2V_{dep}}{d^2} x_0 - \frac{V + V_{dep}}{d} e^{2\mu_h V_{dep} t / d^2} \right]$$

What is the Signal induced on the p+ layer ?



$$x_e(t_e) = d \quad t_e = \frac{d^2}{2\mu_e V_{dep}} \ln \left[\frac{V + V_{dep}}{V - V_{dep}} \left(1 - \frac{x_0}{d} \frac{2V_{dep}}{V + V_{dep}} \right) \right]$$

$$x_h(t_h) = 0 \quad t_h = -\frac{d^2}{2\mu_e V_{dep}} \ln \left(1 - \frac{x_0}{d} \frac{2V_{dep}}{V + V_{dep}} \right)$$

$$E_w(x) = \frac{V_w}{d} \quad i(t) = -\frac{q}{V_w} E_w(x(t)) \frac{dx(t)}{dt}$$

$$i(t) = i_e(t) + i_h(t) = \frac{e_0}{d} \frac{dx_e(t)}{dt} - \frac{e_0}{d} \frac{dx_h(t)}{dt}$$

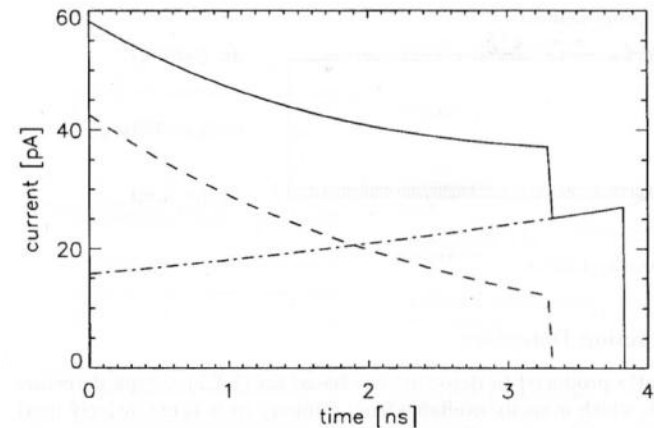
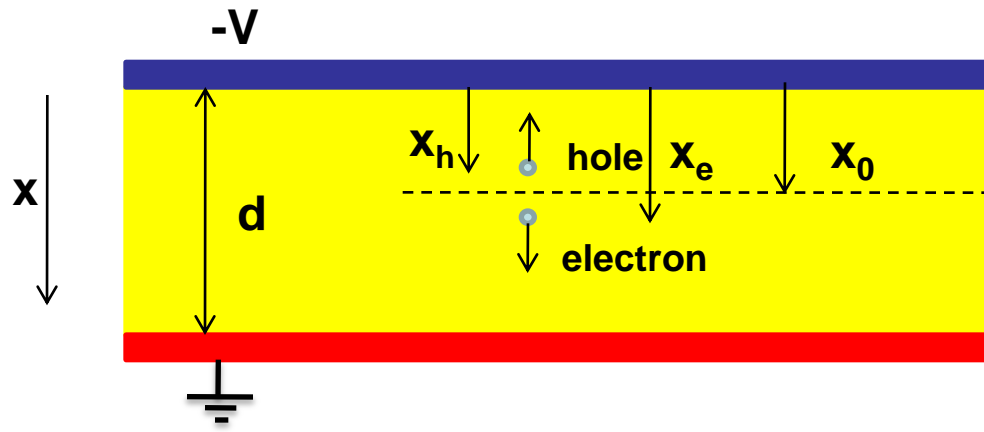


Fig. 5.4. Signal current formation induced by the separation of an electron-hole pair in the electric field of the space-charge region of the detector. The electron-hole pair is created in the center plane of a slightly (20%) overdepleted diode (see Example 5.2). Plotted are the electron-induced (dashed line), hole-induced (dash-dot line) and total (continuous line) currents

What is the Signal induced on the p+ layer ?



p+ What is the signal induced on the p+ 'electrode' for a single e/h pair created at $x_0=d/2$ for a 300 μm Si detector ?

n-

n+

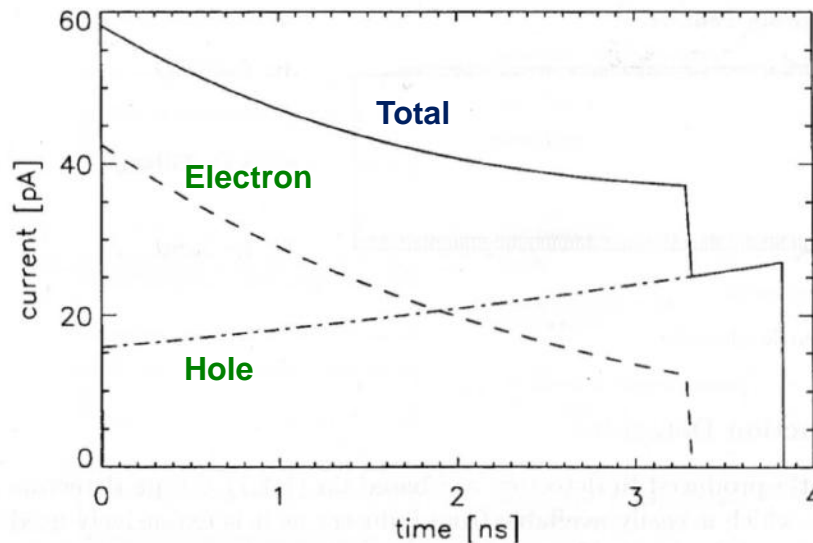


Fig.5.4. Signal current formation induced by the separation of an electron-hole pair in the electric field of the space-charge region of the detector. The electron-hole pair is created in the center plane of a slightly (20%) overdepleted diode (see Example 5.2). Plotted are the electron-induced (dashed line), hole-induced (dash-dot line) and total (continuous line) currents

To calculate the signal from a track one has to sum up all the e/h pair signal for different positions x_0 .

Si Signals are fast $T < 10-15\text{ns}$. In case the amplifier peaking time is $> 20-30\text{ns}$, the induced current signal shape doesn't matter at all.

The entire signal is integrated and the output of the electronics has always the same shape (delta response) with a pulse height proportional to the total deposited charge.

Biassing, AC coupling



Bias resistor and AC Coupling

extra slide
not shown

2b - Tracking with
Solid State Detectors

■ Bias resistor

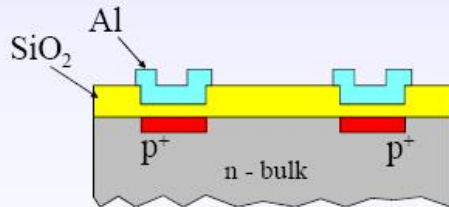
- Need to isolate strips from each other to collect/measure charge on each strip
⇒ high impedance bias connection ($\approx 1\text{M}\Omega$ resistor)

■ Coupling capacitor

- Couple input amplifier through a capacitor (AC coupling) to avoid large DC input from leakage current

■ Integration of capacitors and resistors on sensor

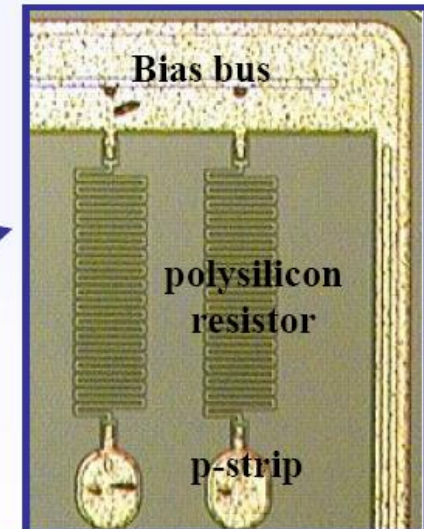
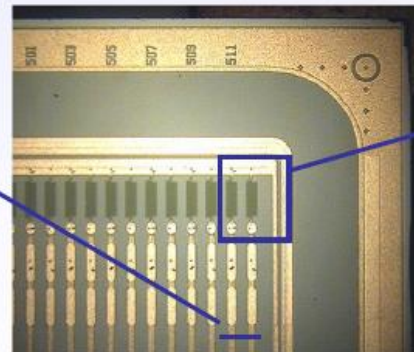
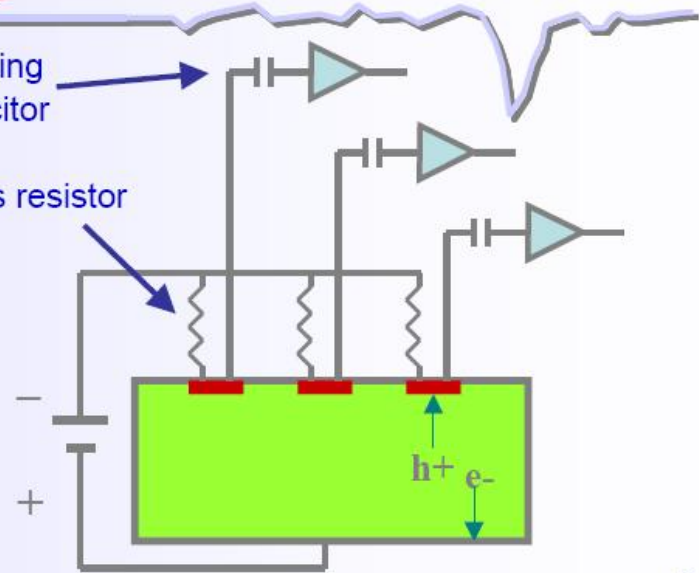
- Bias resistors via deposition of doped polysilicon
- Capacitors via metal readout lines over the implants but separated by an insulating dielectric layer ($\text{SiO}_2, \text{Si}_3\text{N}_4$).



- ⇒ nice integration
- ⇒ more masks, processing steps
- ⇒ pin holes

coupling capacitor

bias resistor



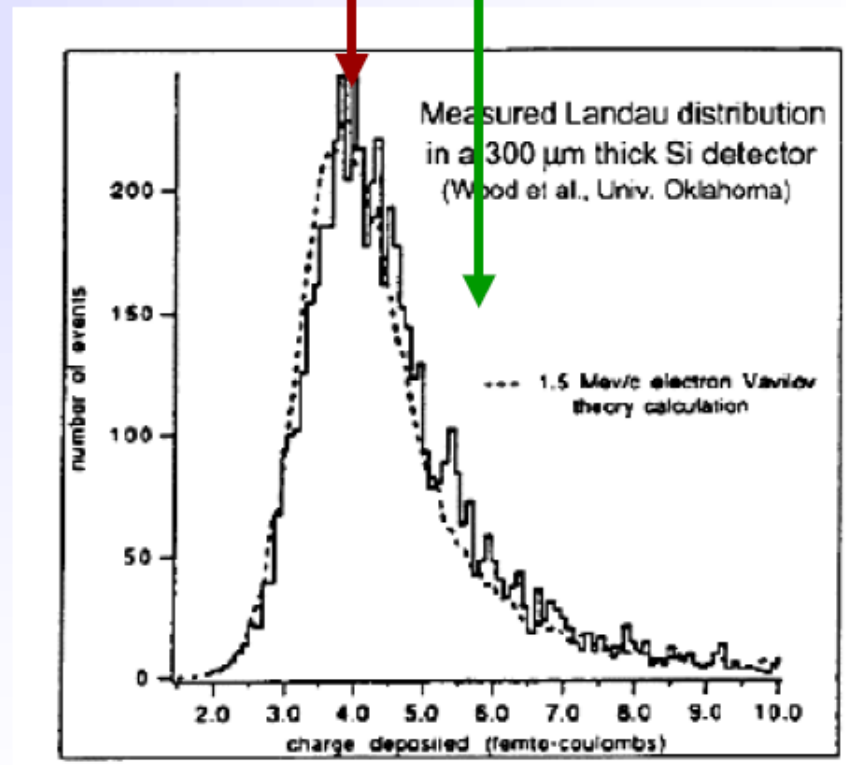
CERN Academic Training Programme 2004/2005

Collected Charge for a Minimum Ionizing Particle (MIP)

- Mean energy loss
 dE/dx (Si) = 3.88 MeV/cm
 \Rightarrow 116 keV for 300 μ m thickness
- Most probable energy loss
 $\approx 0.7 \times$ mean
 \Rightarrow 81 keV
- 3.6 eV to create an e-h pair
 \Rightarrow 72 e-h / μ m (mean)
 \Rightarrow 108 e-h / μ m (most probable)
- Most probable charge (300 μ m)
 ≈ 22500 e ≈ 3.6 fC

Most probable charge $\approx 0.7 \times$ mean

Mean charge



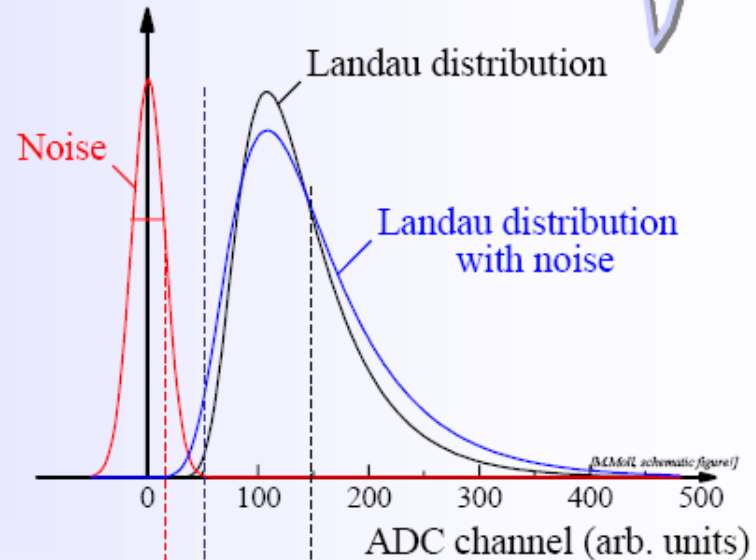
- Landau distribution has a low energy tail
 - becomes even lower by noise broadening

Noise sources: (ENC = Equivalent Noise Charge)

- Capacitance $ENC \propto C_d$

- Leakage Current $ENC \propto \sqrt{I}$

- Thermal Noise (bias resistor) $ENC \propto \sqrt{k_B T / R}$



- Good hits selected by requiring $N_{ADC} > \text{noise tail}$
 - If cut too high \Rightarrow efficiency loss
 - If cut too low \Rightarrow noise occupancy

Figure of Merit: Signal-to-Noise Ratio S/N

- Typical values $>10-15$, people get nervous below 10. Radiation damage severely degrades the S/N.

Charge Collection time

- Drift velocity of charge carriers $v \approx \mu E$, so drift time, $t_d = d/v = d/\mu E$

Typical values: $d=300 \mu\text{m}$, $E= 2.5 \text{ kV/cm}$,
with $\mu_e= 1350 \text{ cm}^2/\text{V}\cdot\text{s}$ and $\mu_h= 450 \text{ cm}^2/\text{V}\cdot\text{s}$

$$\Rightarrow t_d(e) = 9\text{ns}, t_d(h) = 27\text{ns}$$

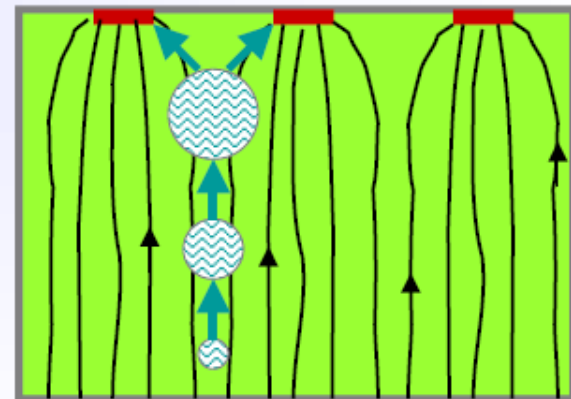
Diffusion

- Diffusion of charge “cloud” caused by scattering of drifting charge carriers, radius of distribution after time t_d :

$$\sigma = \sqrt{2Dt_d} \quad \text{with diffusion constant } D = \mu kT/q$$

- Same radius for e and h since $t_d \propto 1/\mu$

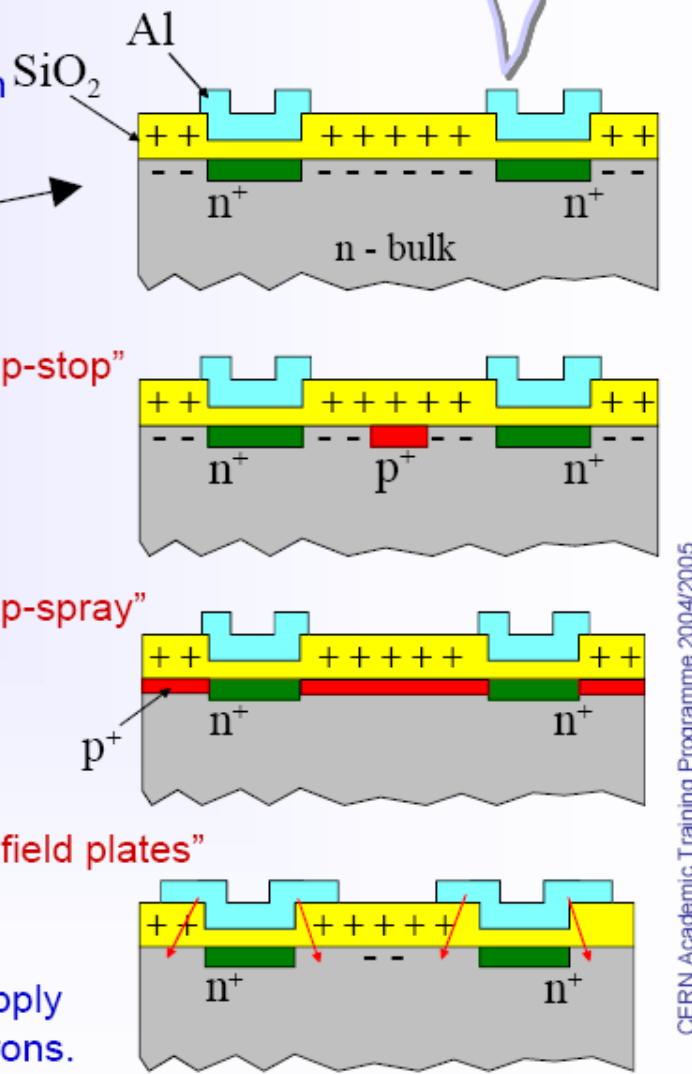
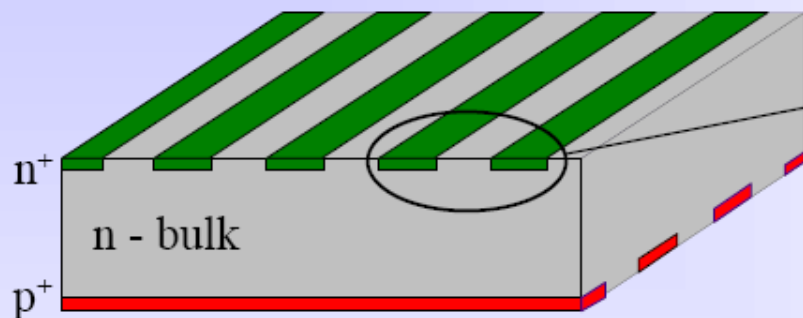
Typical charge radius: $\sigma \approx 6\mu\text{m}$, could exploit this to get better position resolution due to charge sharing between adjacent strips (using centroid finding), but need to keep drift times long (low field).



extra slide
not shown

■ **Get a 2nd coordinate**

Put n⁺ and p⁺ strips on opposite sides and read them both



■ **Problem: Electron accumulation layer**

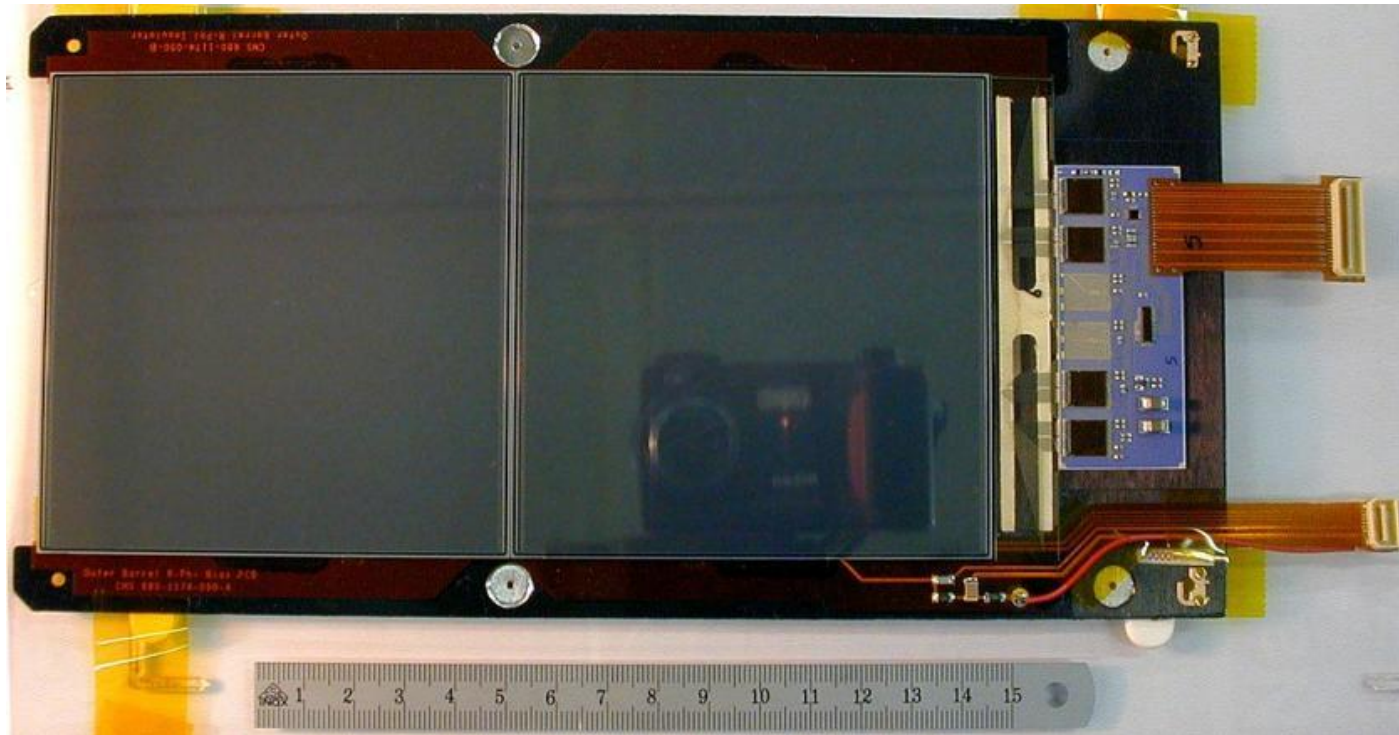
n⁺-strips are not isolated because of an electron accumulation layer at the Si-SiO₂ interface. This effect is due to the presence of positive charge in SiO₂ layer which attracts electrons.

■ **Solution: "Break" accumulation layer**

- p-strips in between the n-strips ("**p-stop**")
- moderate p⁺-implantation over all surface ("**p-spray**")
- "**field plates**" (metal over oxide) over the n⁺-strips and apply negative potential with respect to n⁺-strips to repel electrons.

Picture of an CMS Si-Tracker Module

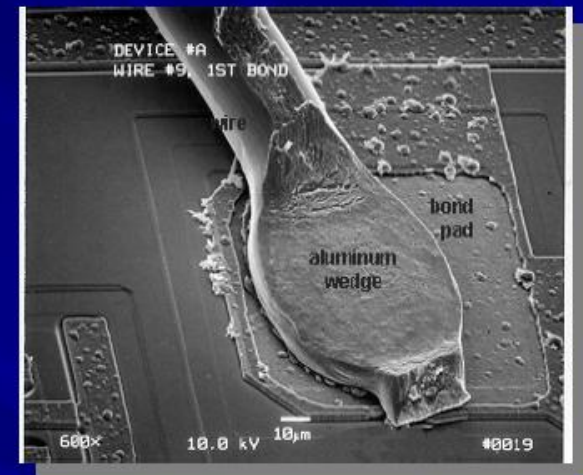
Outer Barrel Module



Wire Bonding

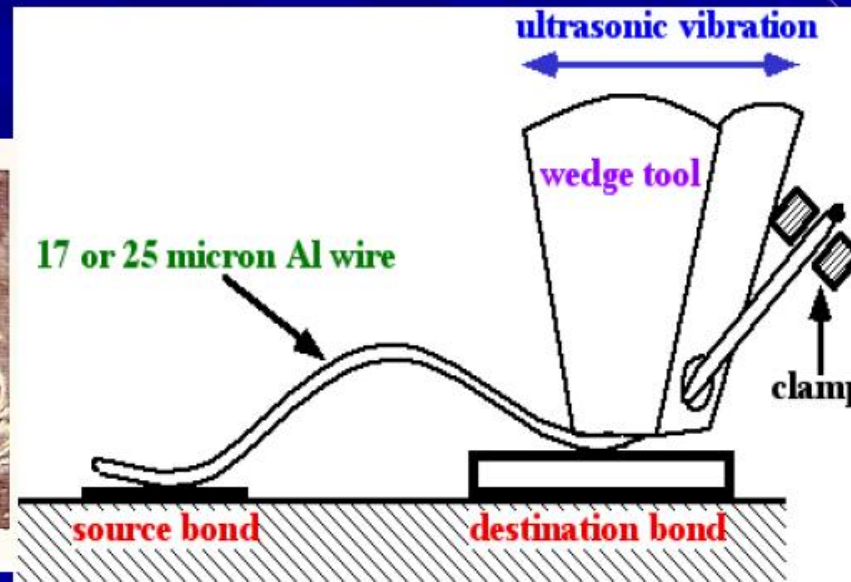
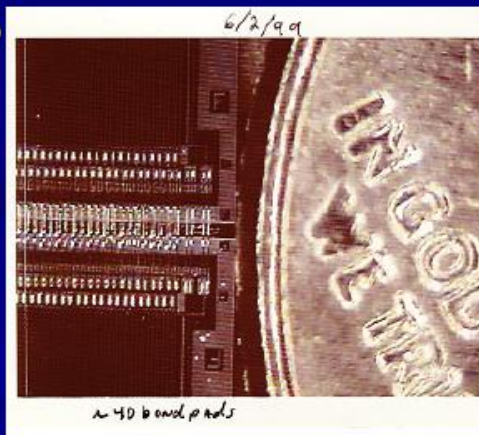
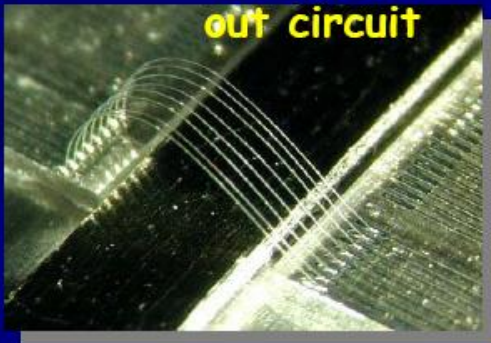
- Ultrasonic power is used to vibrate needle-like tool on top of Al wire. Friction welds wire to metallized substrate underneath.
- Pitch: $80\mu\text{m}$ pitch in a single row and $40\mu\text{m}$ in two staggered rows (typical FE chip pitch is $\approx 44\mu\text{m}$).
- $\approx 25\mu\text{m}$ diameter aluminum wire and bond to aluminum pads (chips) or gold pads (hybrid substrates).
- Used in industry (PC processors) but not with such thin wire or small pitch.

Electron micrograph of bond "foot"

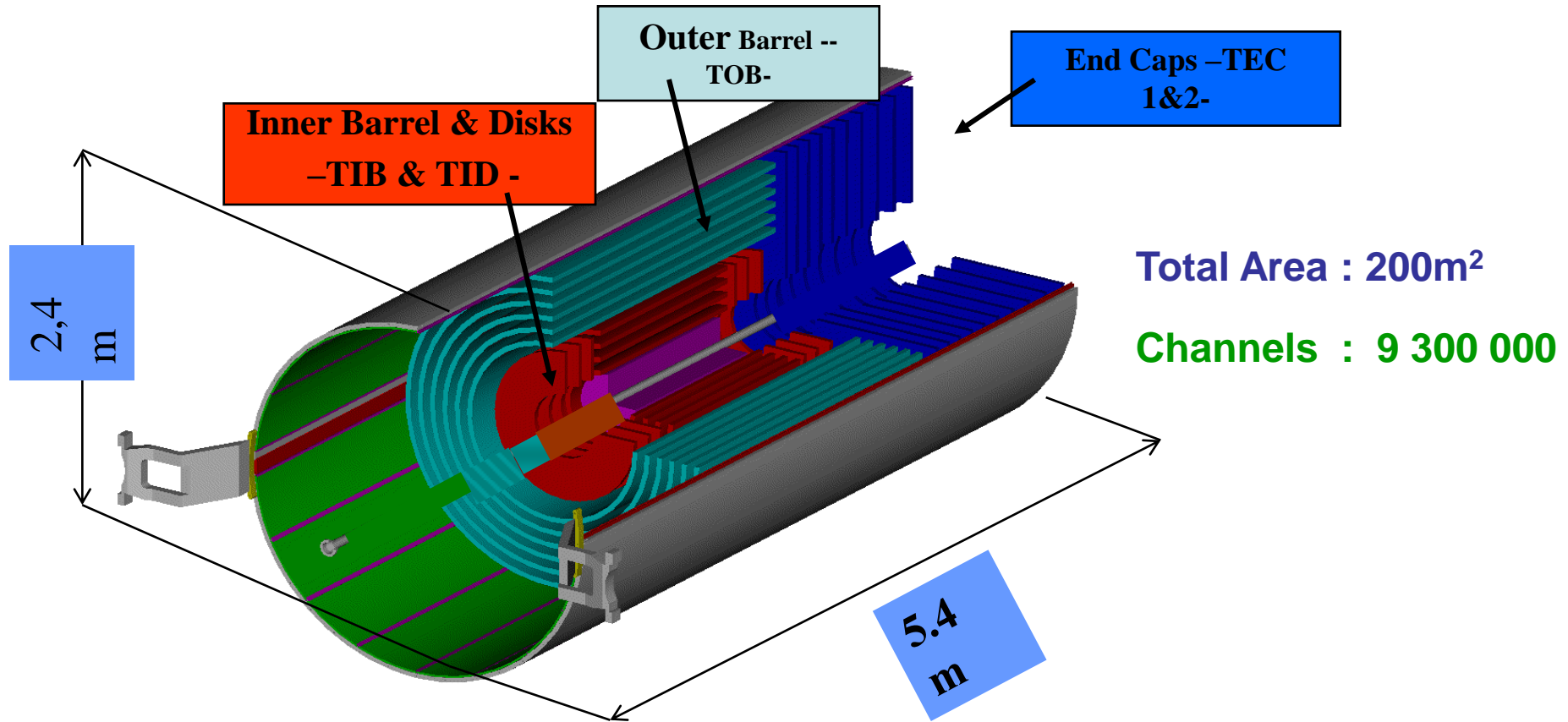


View through microscope of wire bonds connecting sensor to

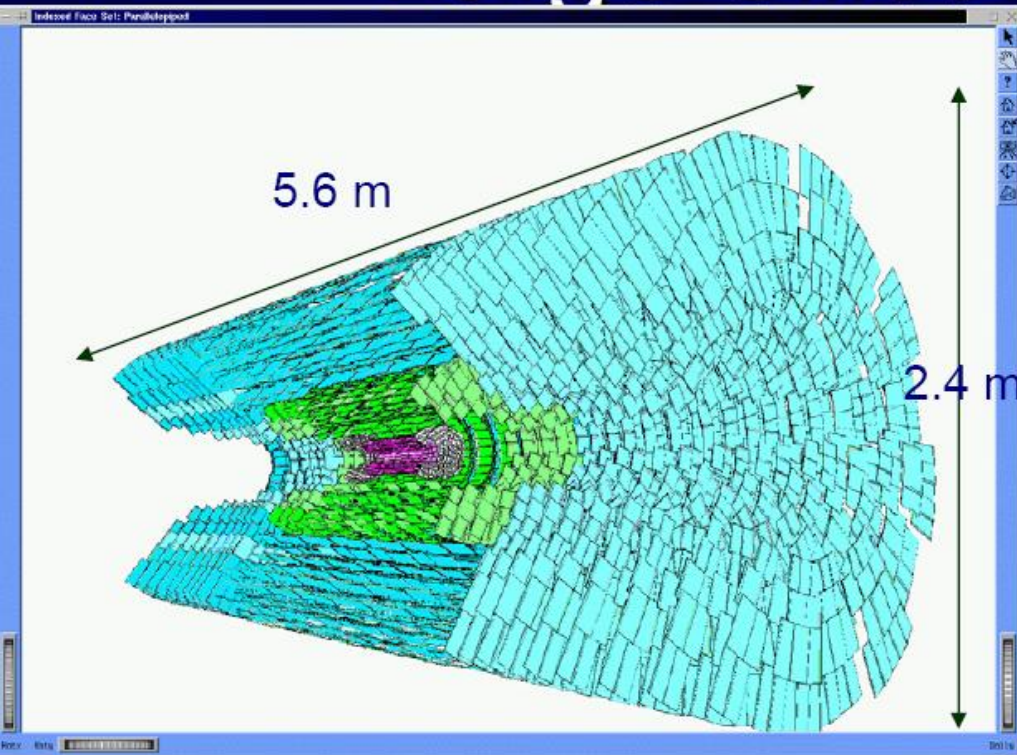
out circuit



CMS Tracker Layout



Large Silicon Systems



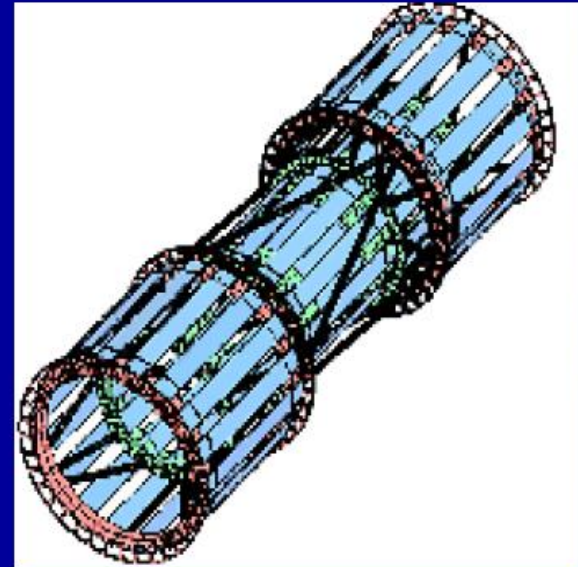
CMS tracker (~2007)

12000 modules

~ 445 m² silicon area

~ 24,328 silicon wafers

~ 60 M readout channels

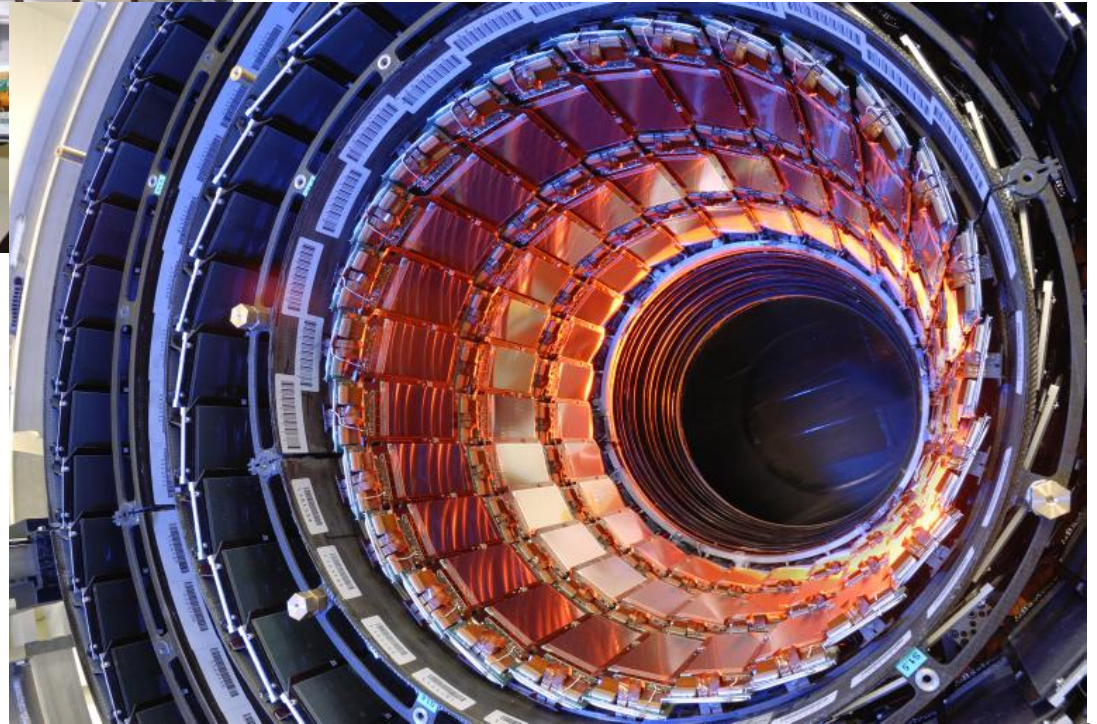


CDF SVX IIa (2001-)

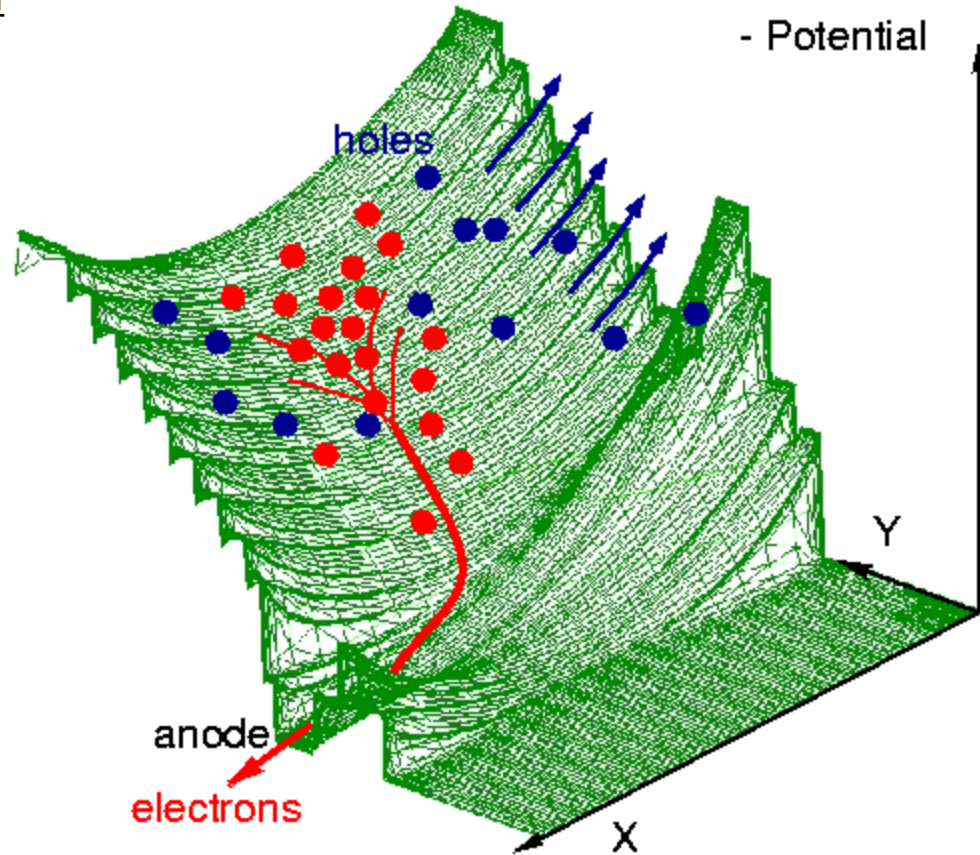
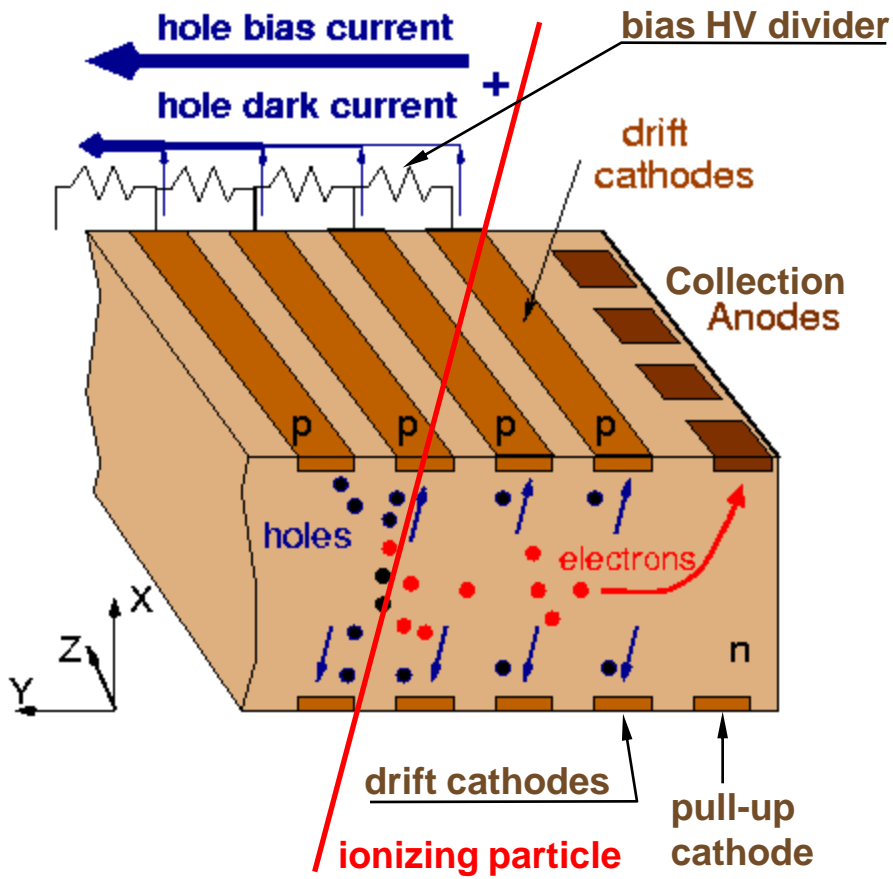
~ 11m² silicon area

~ 750 000 readout channels

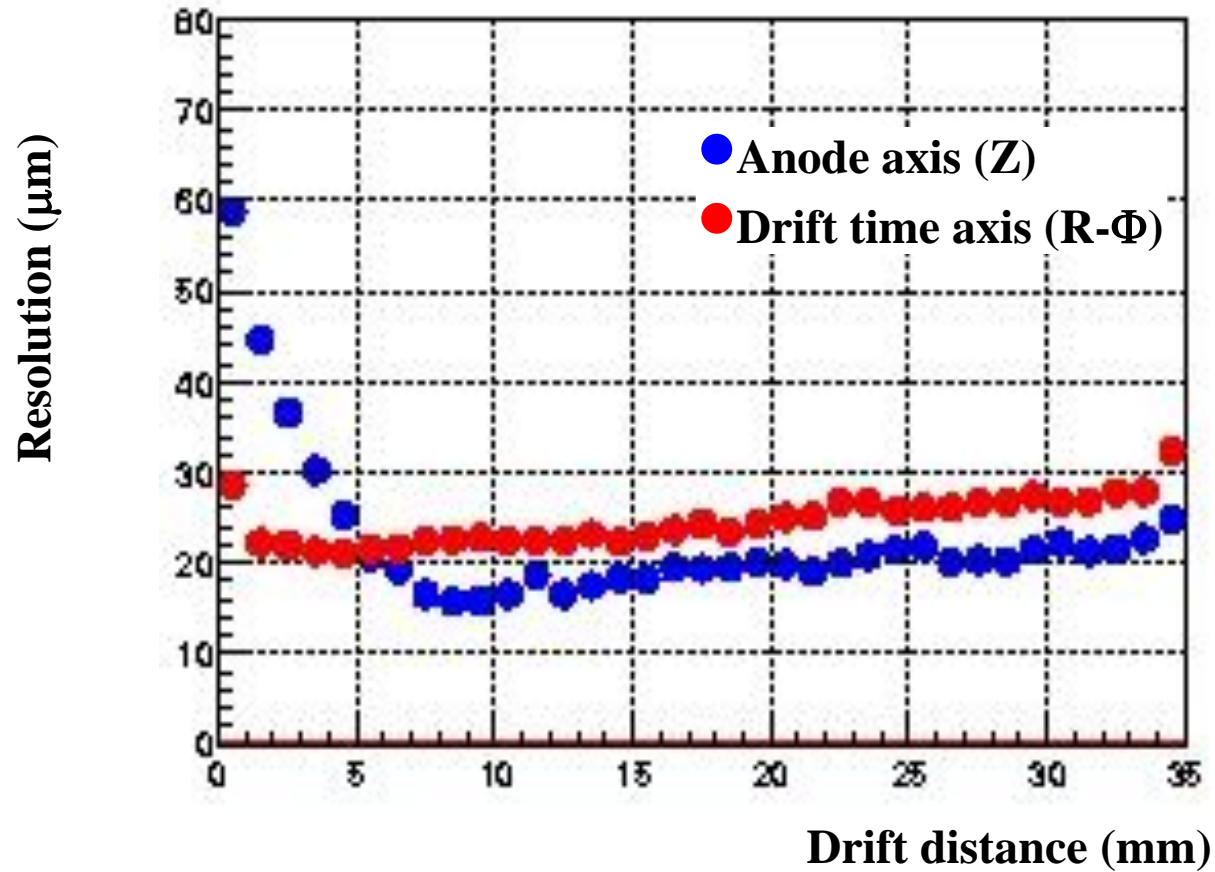
CMS Tracker



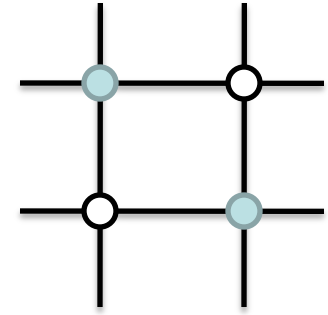
Silicon Drift Detector (like gas TPC !)



Silicon Drift Detector (like gas TPC !)



Pixel-Detectors



Problem:

2-dimensional readout of strip detectors results in 'Ghost Tracks' at high particle multiplicities i.e. many particles at the same time.

Solution:

Si detectors with 2 dimensional 'chessboard' readout. Typical size 50 x 200 μm .

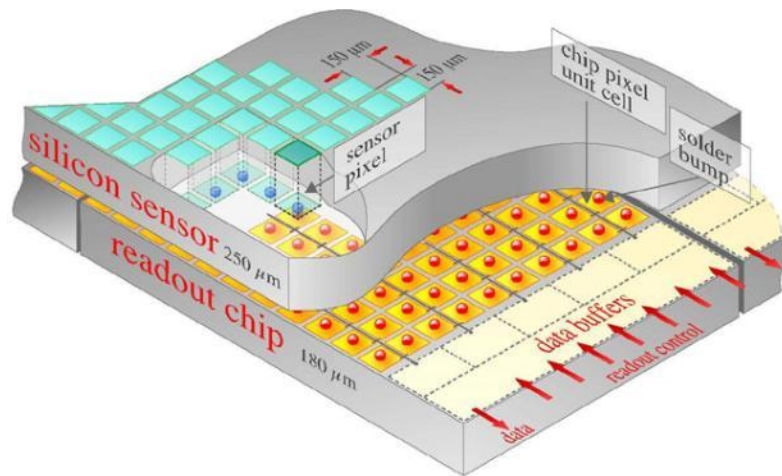
Problem:

Coupling of readout electronics to the detector.

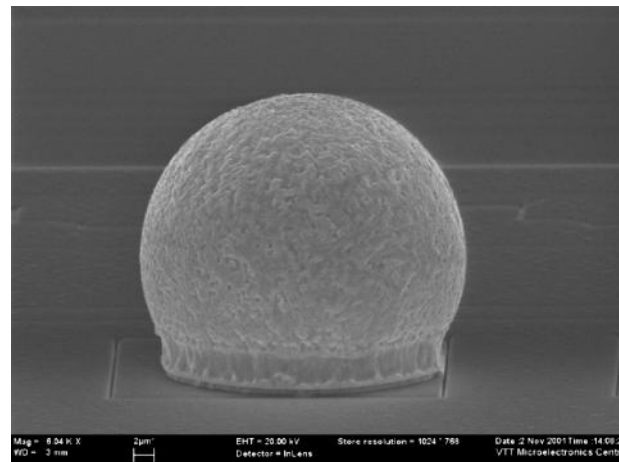
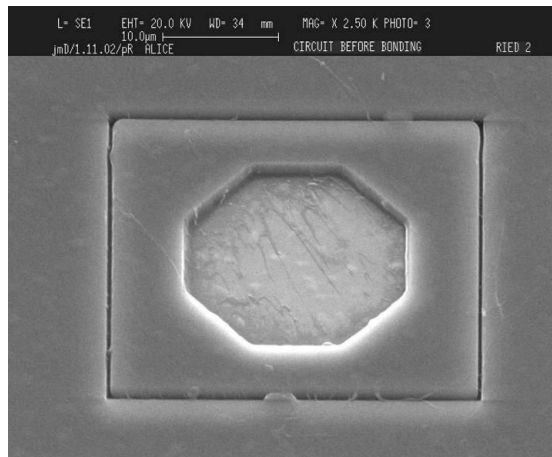
Solution:

Bump bonding.

Bump Bonding of each Pixel Sensor to the Readout Electronics



ATLAS: 1.4×10^8 pixels



Radiation Effects 'Aging'

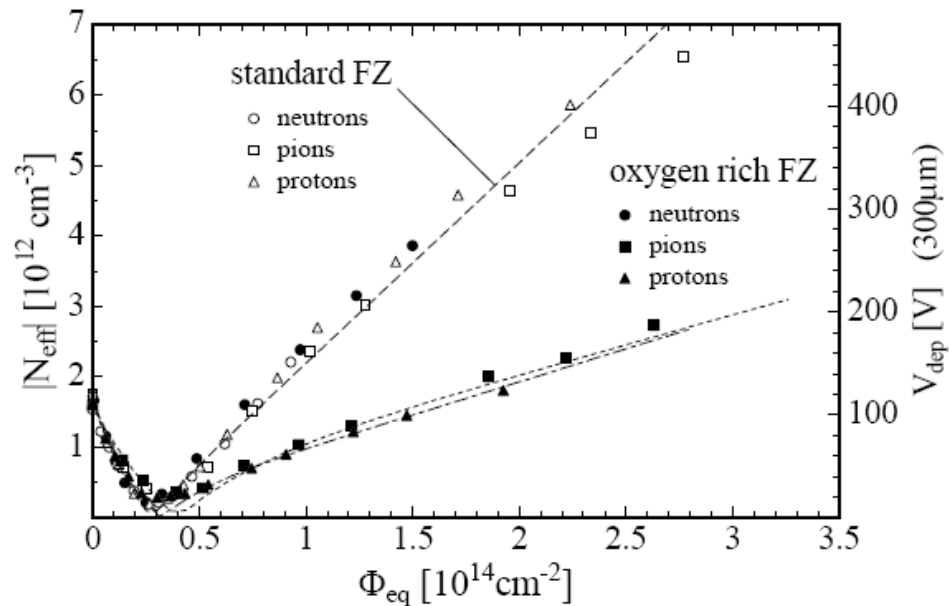
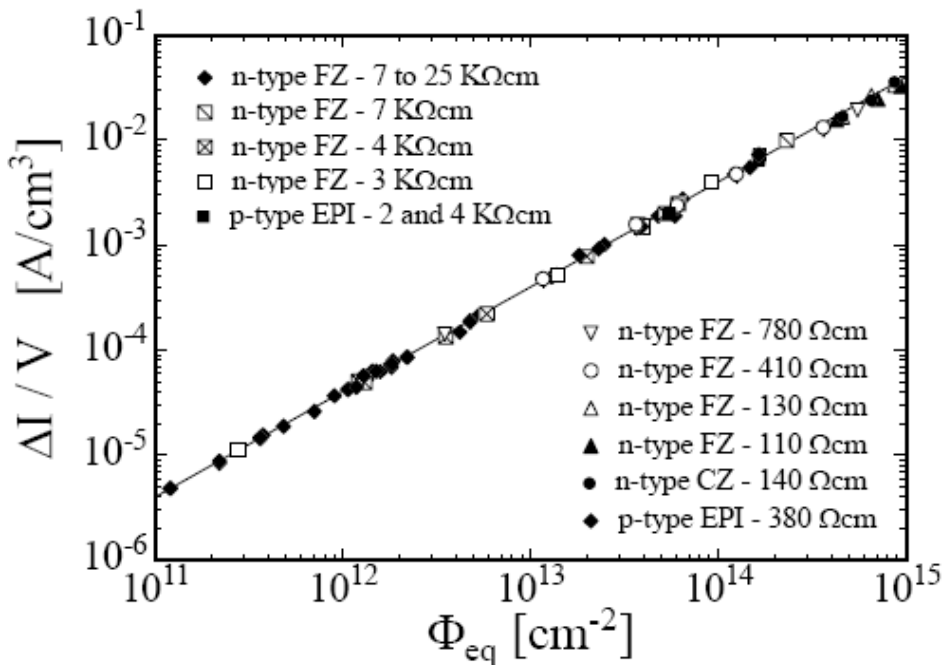
- Two general types of radiation damage
 - "Bulk" damage due to physical impact within the crystal
 - "Surface" damage in the oxide or Si/SiO₂ interface
- Cumulative effects
 - Increased leakage current (increased shot noise)
 - Silicon bulk type inversion (n-type to p-type)
 - Increased depletion voltage
 - Increased capacitance
- Sensors can fail from radiation damage
 - Noise too high to effectively operate
 - Depletion voltage too high to deplete
 - Loss of inter-strip isolation (charge spreading)
- Signal/noise ratio is the quantity to watch

Radiation Effects 'Aging'

Increase in leakage current

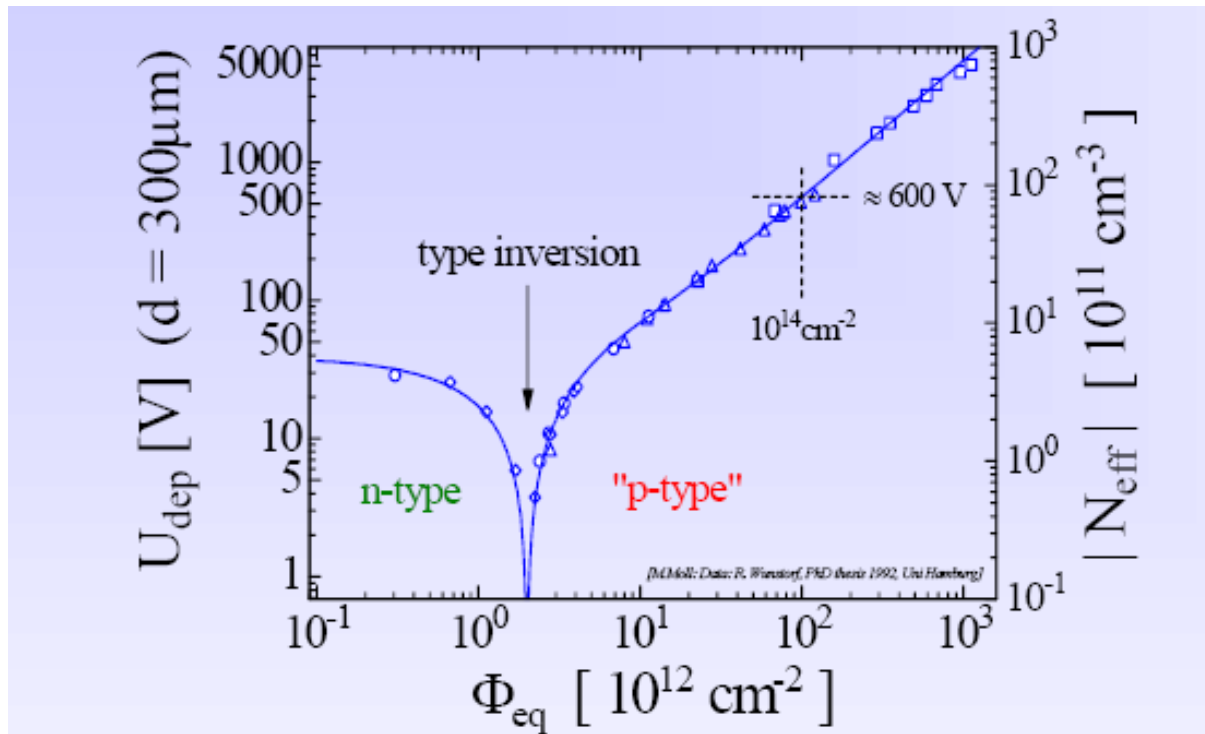
Increase in depletion voltage

Decrease in charge collection efficiency due to underdepletion and charge trapping.



Radiation Effects 'Aging'

Type inversion ! An n-type Si detector becomes a p-type Si detector !



- “Type inversion”: N_{eff} changes from positive to negative (Space Charge Sign Inversion)

Silicon Detectors: towards higher Radiation Resistance

Typical limits of Si Detectors are at 10^{14} - 10^{15} Hadrons/cm²

LHC

- We can identify 3 different regions to match radiation damage and occupancy in the current LHC detector

R	Φ	Technology
>50 cm	10^{13}	p-on-n strip 500 μm thick, high resistivity ($\approx 5 \text{ K}\Omega\cdot\text{cm}$), pitch $\sim 200 \mu\text{m}$
20-50 cm	10^{14}	p-on-n strips 320 μm thick, low resistivity ($\approx 2 \text{ K}\Omega\cdot\text{cm}$), pitch $\sim 80 \mu\text{m}$
<20 cm	10^{15}	n-on-n pixels 270 μm thick sensors low resistivity ($\approx 2 \text{ K}\Omega\cdot\text{cm}$) oxygenated

SLHC

- Radiation fluence increases by about a factor of 10 from one region to the other and by a factor of 10 between LHC and SLHC.

R	Φ	CCE	Technology
>50 cm	10^{14}	20ke	Present rad-hard technology (or n-on-p)
20-50 cm	10^{15}	10ke	Present n+-n LHC pixel (or n-on-p)
<20 cm	10^{16}	>5Ke	RD needed

R&D Strategy:

Defect Engineering
Oxygen enriched Si

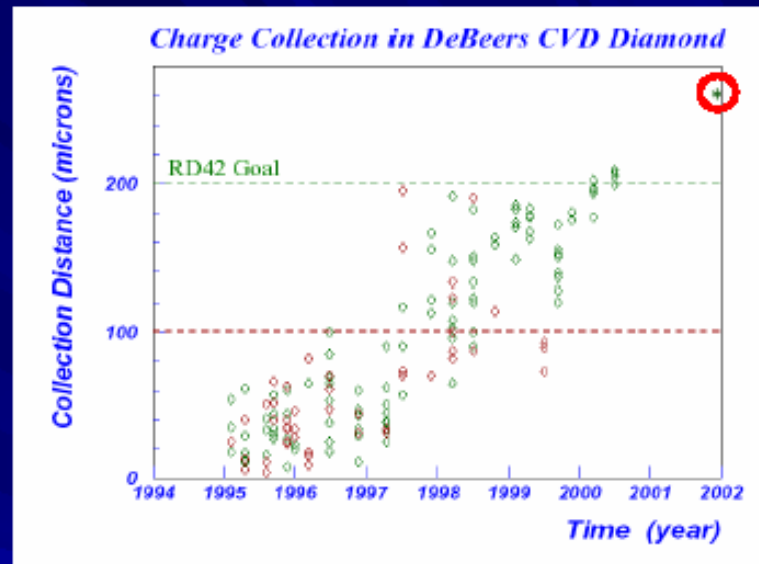
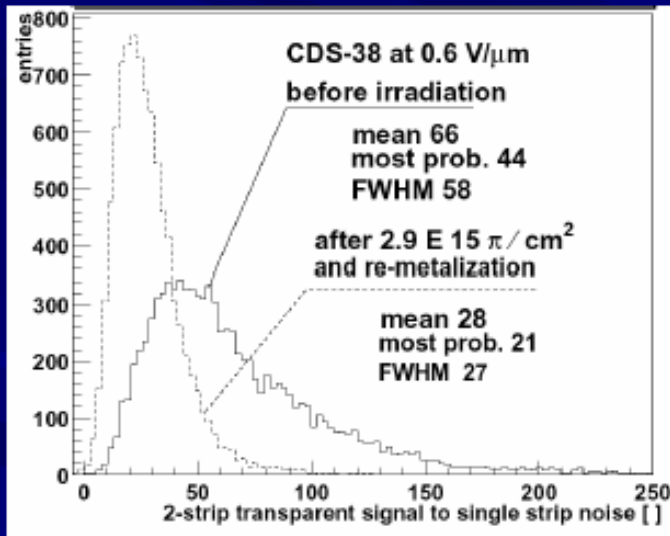
New Materials
Diamonds
Czochralski Si
...

New Geometries

Low Temperature Operation

New Materials: Polycrystalline Diamond

- RD42 in collaboration with Element Six have achieved impressive improvements in collection distances
- pCVD structures show good radiation hardness



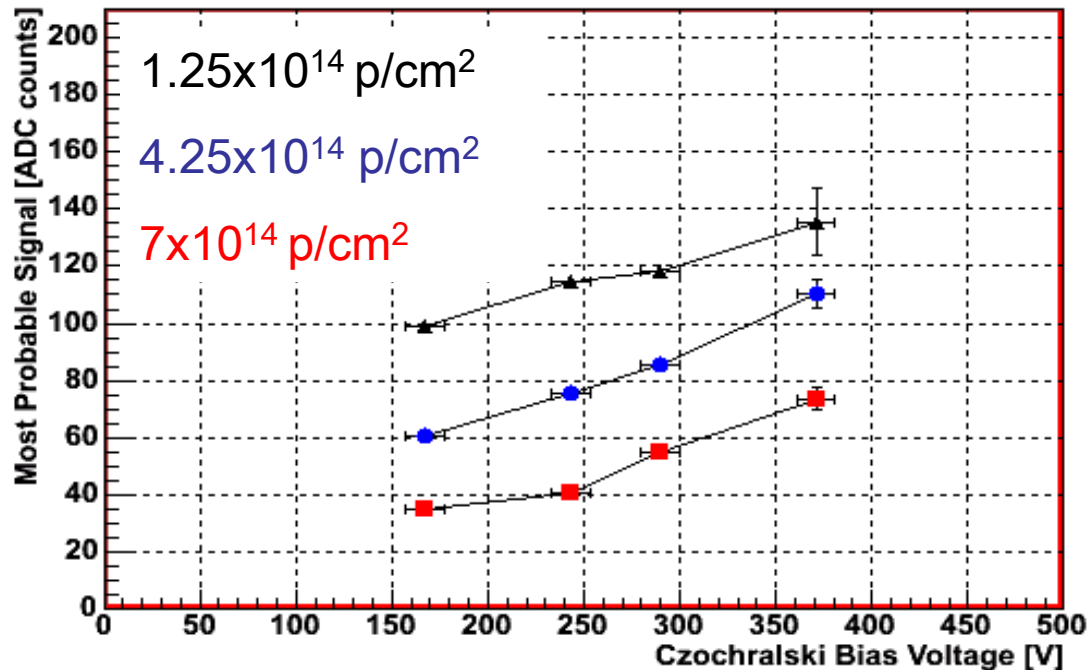
52% loss of S/N at $2.9 \text{ E } 15 \pi / \text{cm}^2$
23% improvement in resolution

Application:

- Used in successfully for radiation monitoring for BaBar (see Kagan's talk at Vertex 2003)

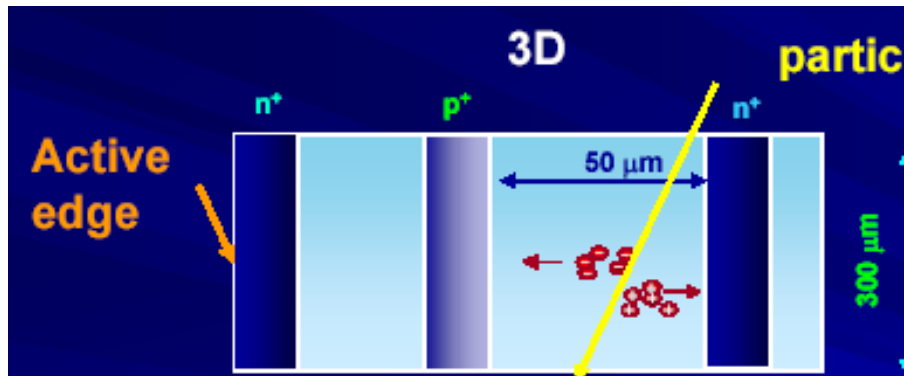
New Material: Czochralski Silicon

Most Probable Signal as a function of Bias Voltage

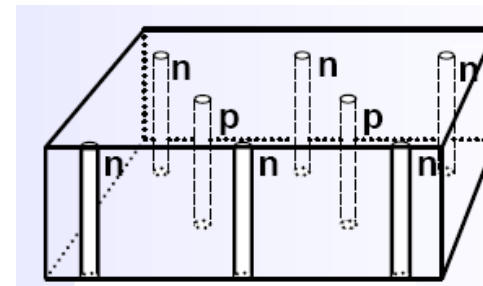


Due to 1000 times higher Oxygenation levels compared to standard Si: expect improved Radiation Resistance

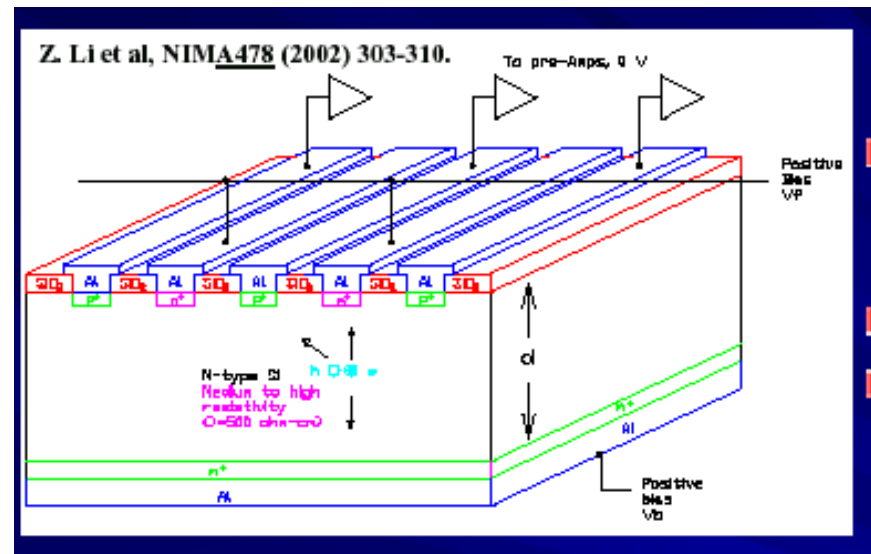
New Geometries: '3D' Si Detectors



	3D	Planar
Q collection path	50µm	300 µm
V _{depletion}	<10V	70 V
Edge sensitivity	10µm	500 µm
Q Collection time	1-2 ns	10-20 ns



[Proposed: S.I. Parker et al.,
NIMA 395 (1997) 328]



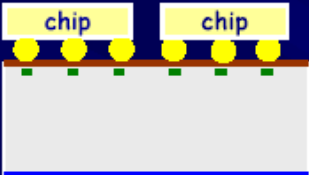
Good Performance after 10^{15} p/cm²

High Resolution Low Mass Silicon Trackers, Monolithic Detectors


Linear Collider Physics requirement:

$$\delta (\text{IP}) < 5 \mu\text{m} \oplus 10 \mu\text{m}/(\rho \sin^{3/2} \theta)$$


(best SLD $8 \mu\text{m} \oplus 33 \mu\text{m}/(\rho \sin^{3/2} \theta)$)



Hybrid Active Pixel: Chip bump bonded to sensor
RD: make it thinner (LHC sensors 2% X_0 /layer), improve space point resolution with interleaved pixels

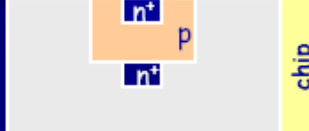


CCD: charge collected in thin layer and transferred through silicon
RD: readout speed, radiation hardness, material support



CMOS sensors (MAPS, FAPS): standard CMOS wafer integrates all functions.
RD: fast readout, non-standard technologies

Poster by Deptuch on Mimosa



DEPFET, CMOS on SOI (talk by Kucewiz) :
Fully depleted sensor with integrated preamp
RD: pixel size, power, thinning, speed

Large variety of monolithic pixel Detectors explored, mostly adapted to low collision rates of LC.

Summary on Solid State Detectors

Solid state detectors provide very high precision tracking in particle physics experiments (down to 5 μ m) for vertex measurement but also for momentum spectroscopy over large areas (CMS).

Technology is improving rapidly due to rapid Silicon development for electronics industry.

Typical number where detectors start to strongly degrade are 10^{14} - 10^{15} hadron/cm².

Diamond, engineered Silicon and novel geometries provide higher radiation resistance.

Clearly, monolithic solid state detectors are the ultimate goal. Current developments along these lines are useful for low rate applications. ar